

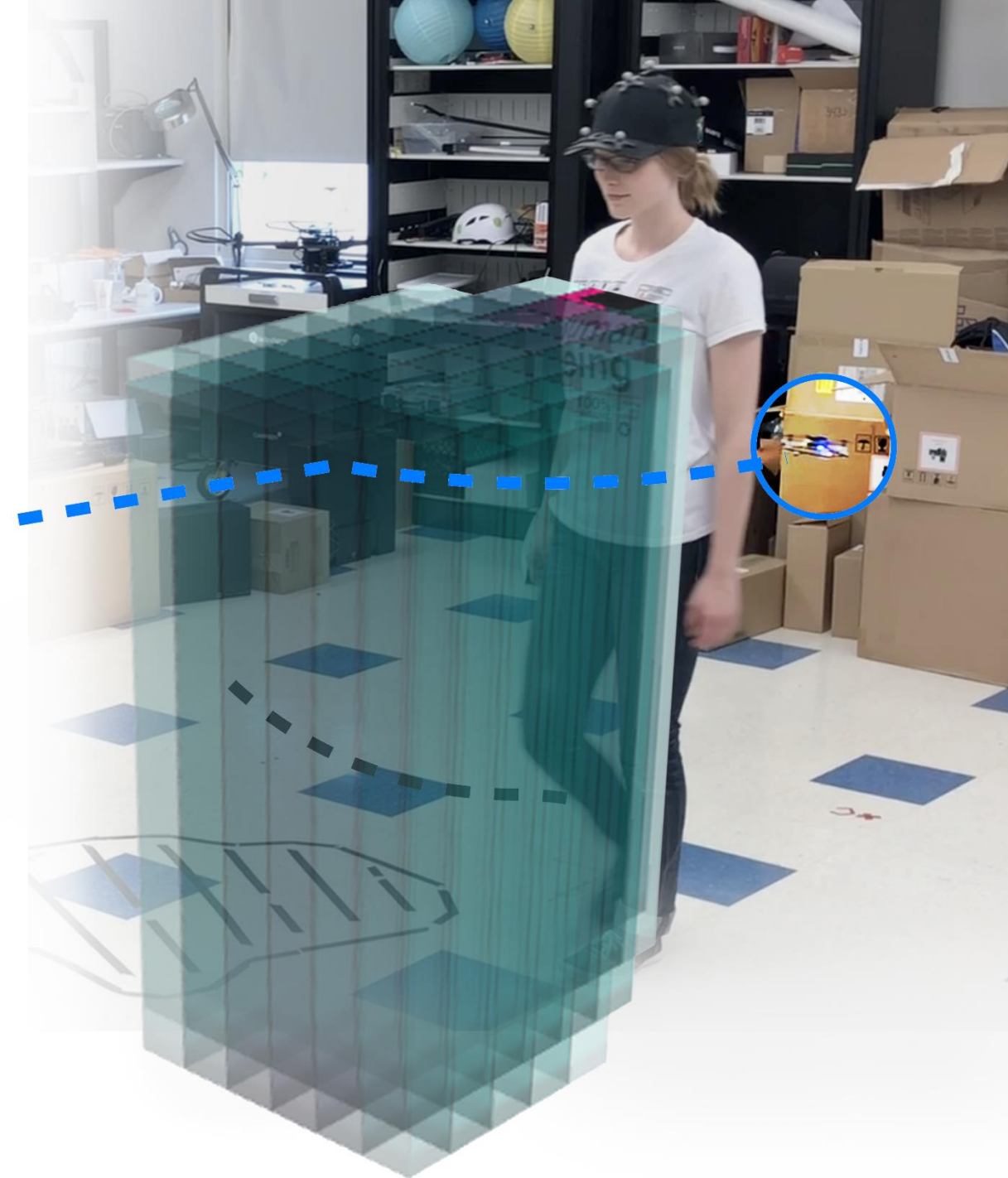
Confidence-aware motion prediction for real-time collision avoidance

Andrea Bajcsy

Long-term Human Motion Prediction Workshop

ICRA 2019

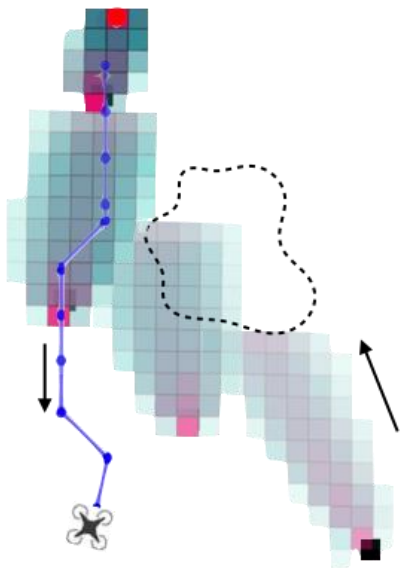
Work with Sylvia Herbert, Jaime Fisac, David Fridovich-Keil, Steven Wang, Sampada Deglurkar, Claire Tomlin and Anca Dragan



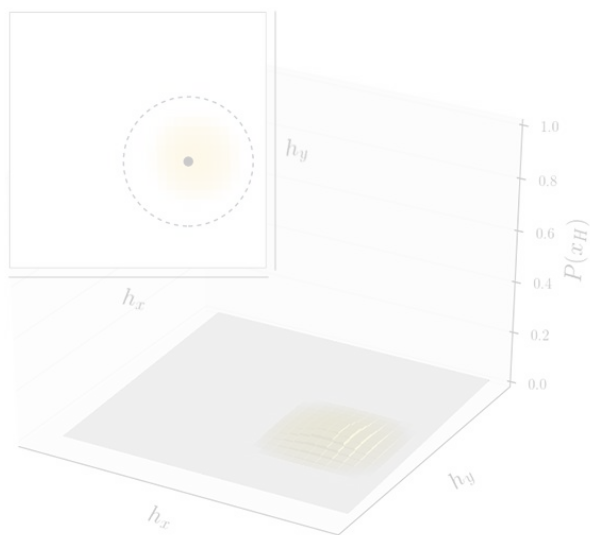


When robots observe behavior that is not well explained by their predictive models, how do they produce **safe** but **efficient** motions?

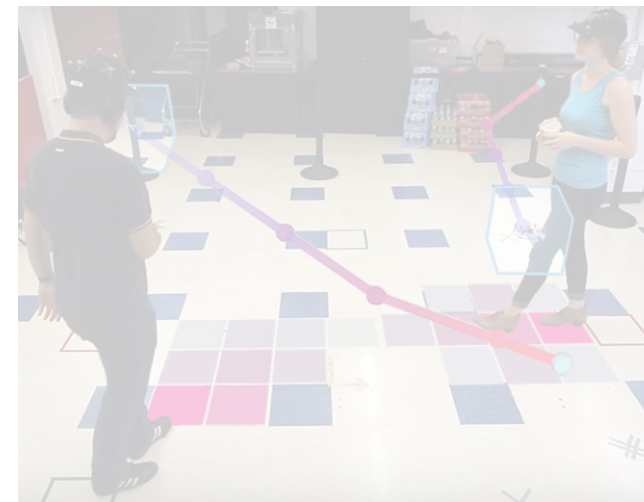
Confidence-aware prediction & planning



Connections to reachability analysis

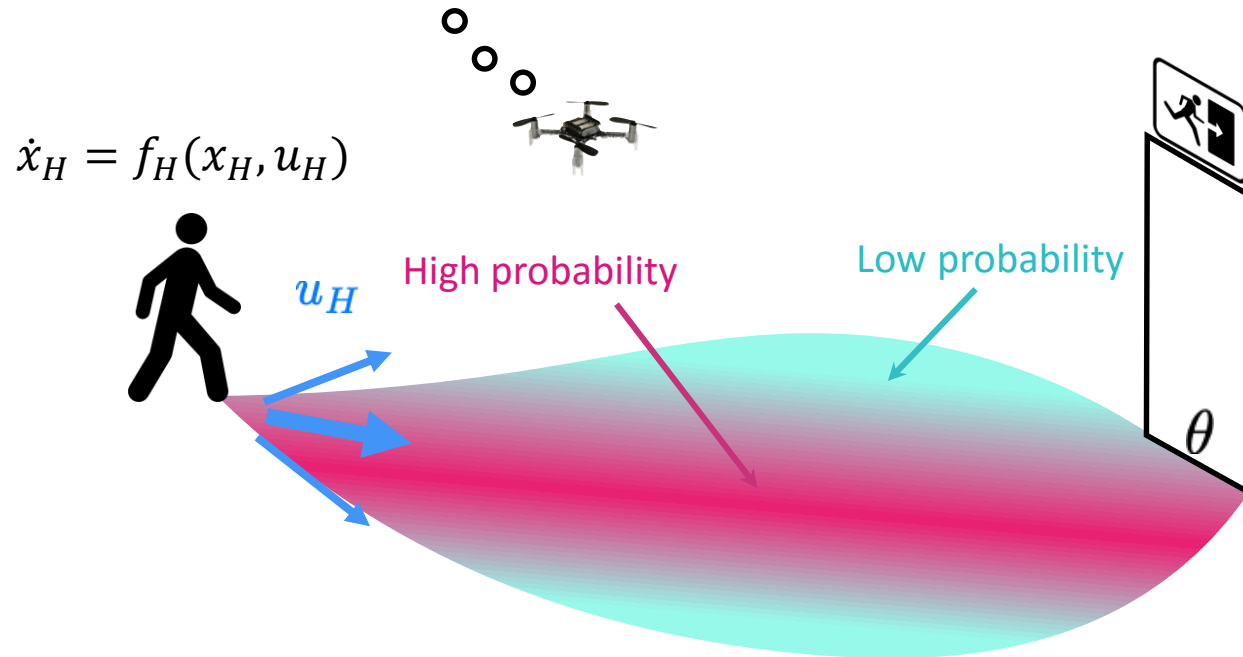


Scaling up to multi-robot, multi-human scenarios



Noisily-Rational Human Motion Prediction

$$P(u_H | x_H; \theta, \beta) \propto e^{\beta Q(x_H, u_H; \theta)}$$



[Luce, 1959]

[Baker et al., 2007]

[Schultz et al., ICRA 2017]

[Pfeiffer et al., IROS 2016]

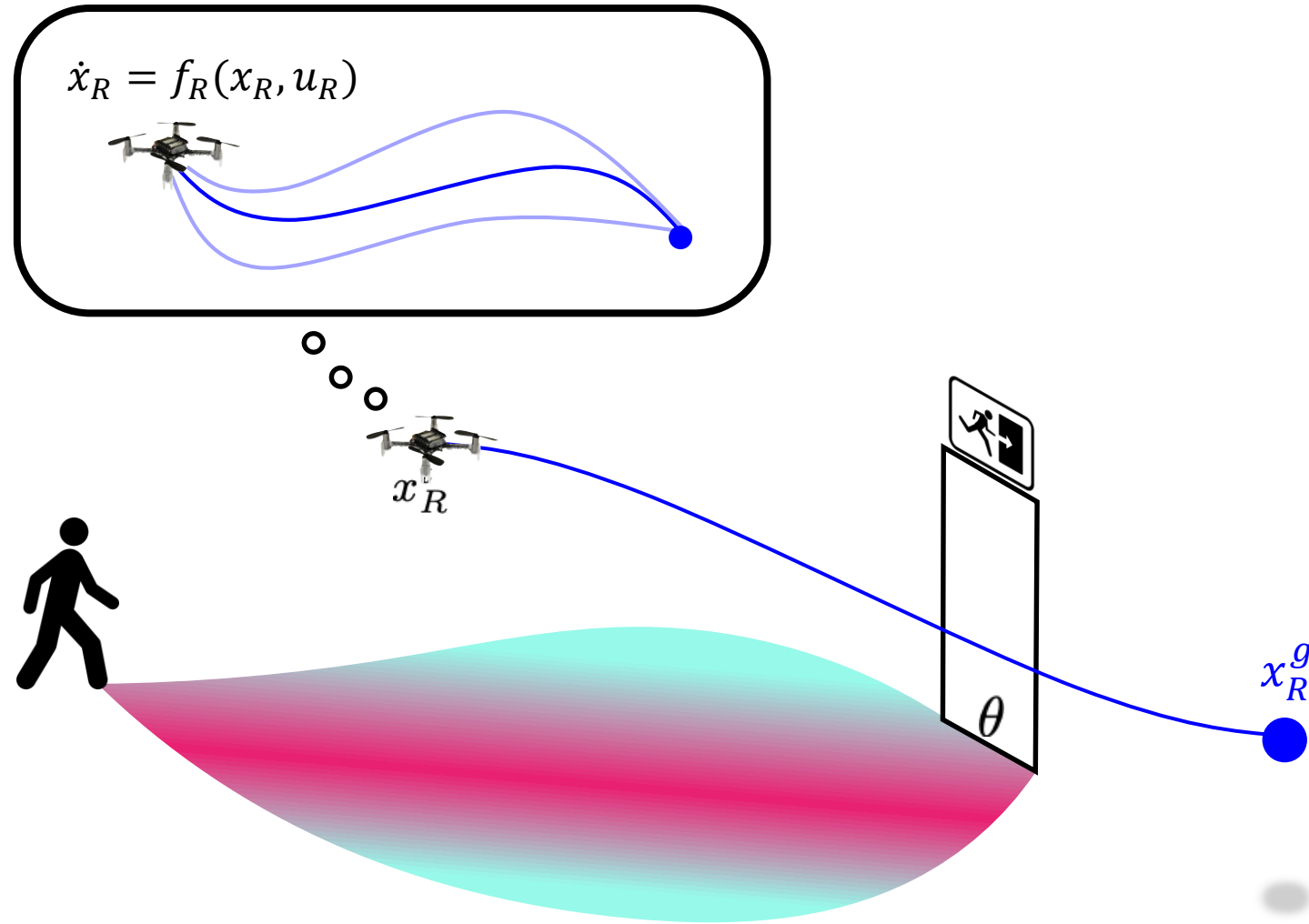
[Finn et al., ICML 2016]

[Herman et al., ICRA 2015]

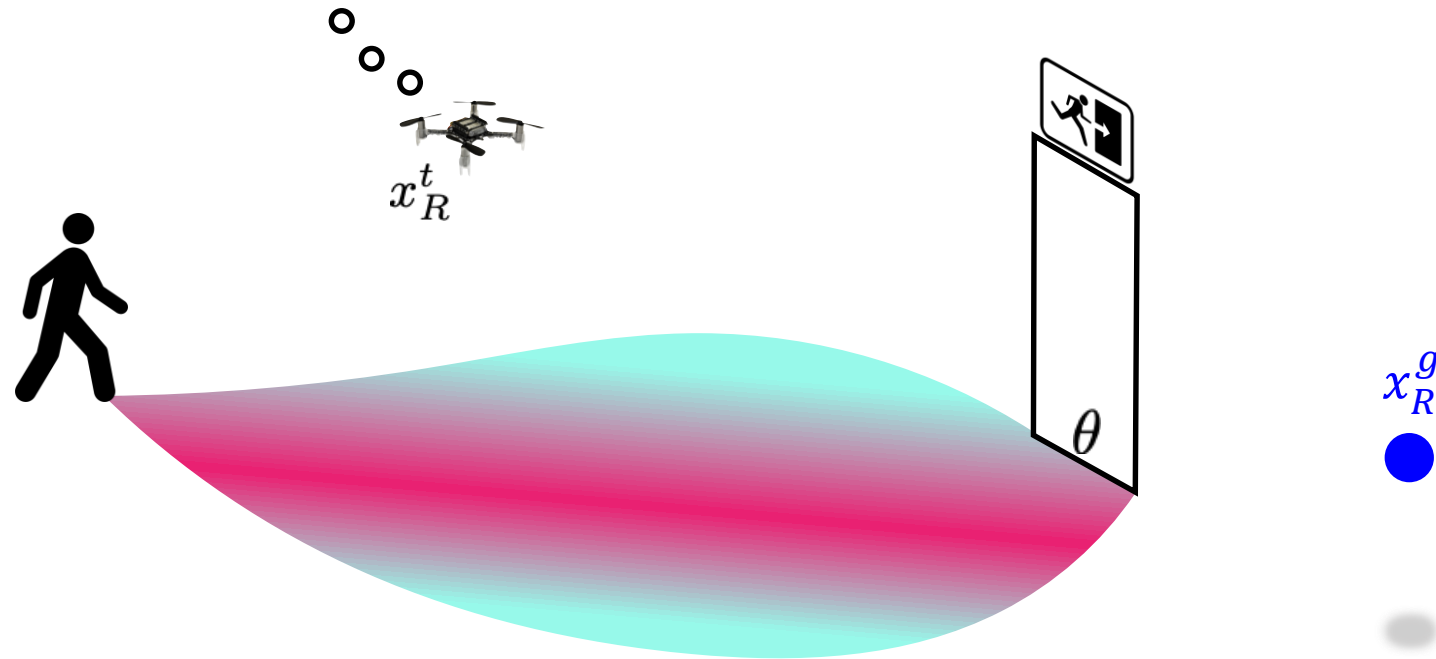
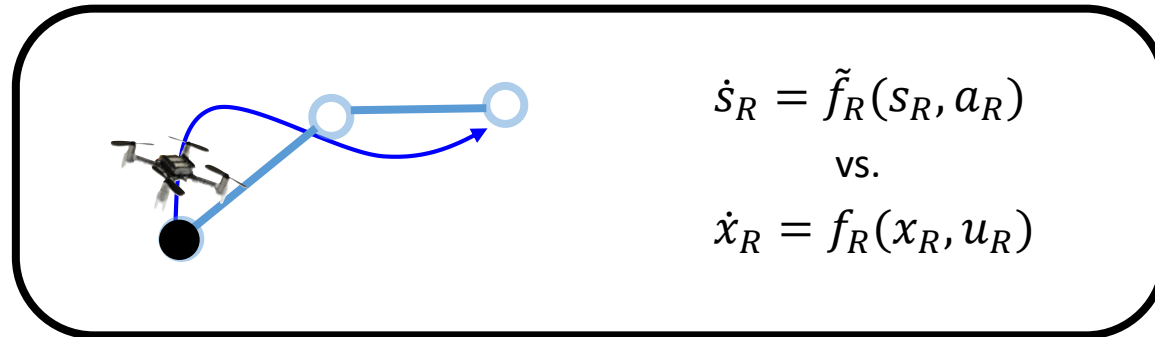
[Ziebart et al., AAAI 2008]

[Ramachandran et al., IJCAI 2007]

Robust Robot Planning with Human Predictions



Robust Robot Planning with Human Predictions

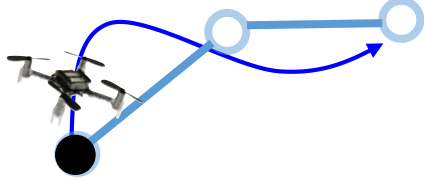


[Lygeros, 2005]

[Mitchell, 2005]

[Herbert, 2017]

Robust Robot Planning with Human Predictions

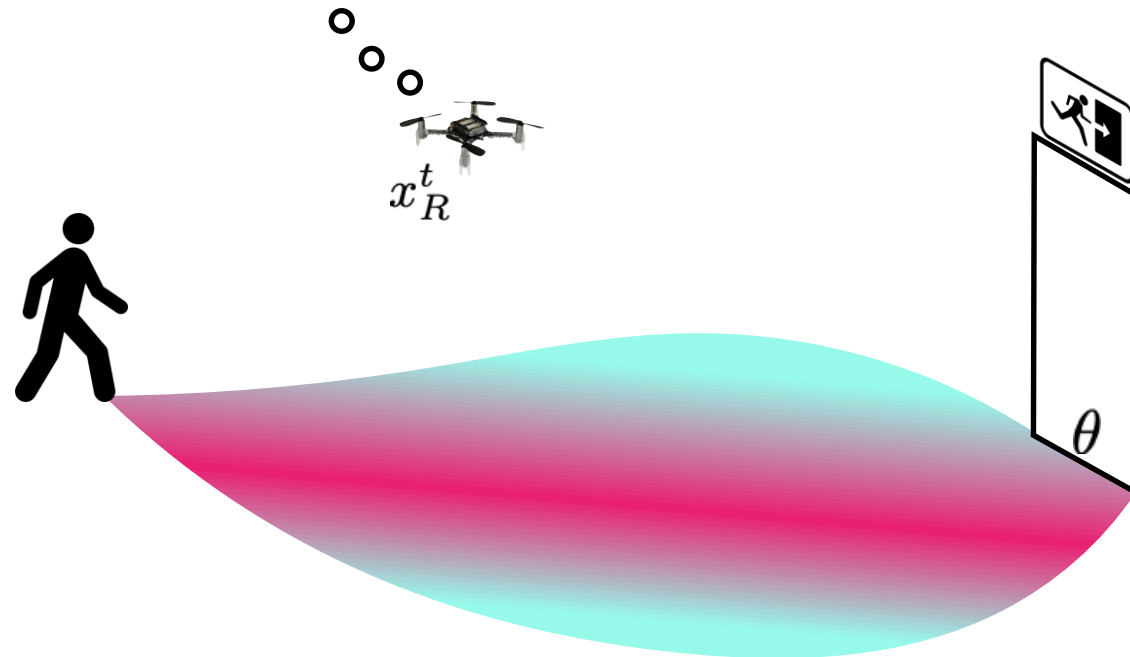


Hamilton-Jacobi Reachability Analysis

$$S_R = \int_R(S_R, a_R)$$

$$\dot{r} = f_R(x_R, u_R) - \phi(f_R(S_R, a_R))$$

vs.

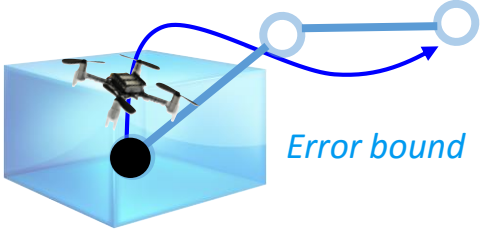
$$V(r, T) = \sup_{x_R^t \in f_R^{-1}(0)} \inf_{u_R} \{ \sup_{\xi^u} \text{cost}(\xi^u, a(t)) \}$$


[Lygeros, 2005]

[Mitchell, 2005]

[Herbst, 2017] [Herbst, Chen*, Han, Bansal, Fisac, Tomlin. "FaSTrack: a Modular Framework for Fast and Guaranteed Safe Motion Planning." CDC, 2017.]

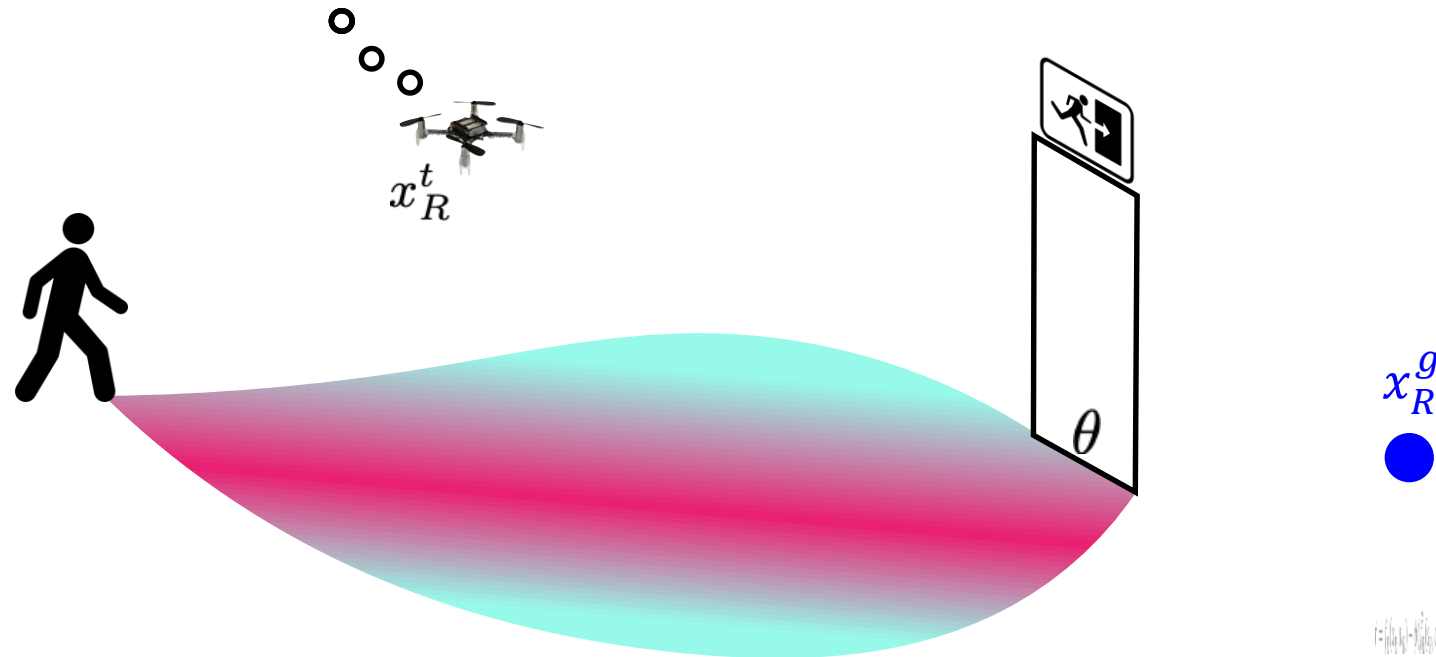
Robust Robot Planning with Human Predictions



Hamilton-Jacobi Reachability Analysis

$$\dot{r} = f_R(x_R, u_R) - \phi(\tilde{f}_R(s_R, a_R))$$
$$V(r, T) = \sup_{a[u](\cdot)} \inf_{u(\cdot)} \{ \sup_{t \in [0, T]} \text{cost}(\xi_r^{u, a}(t)) \}$$

Error bound

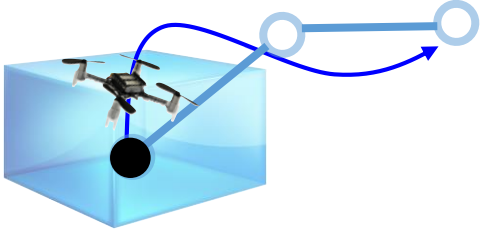


[Lygeros, 2005]

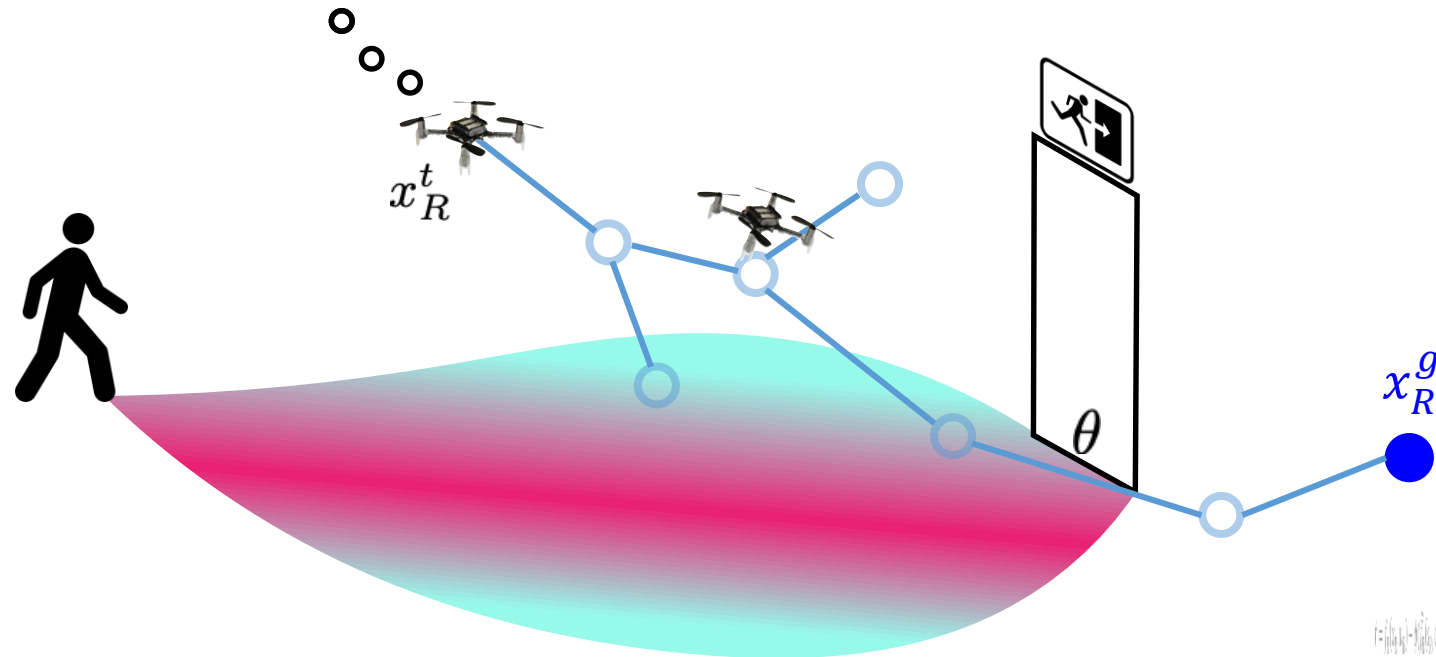
[Mitchell, 2005]

[Herbert*, Chen*, Han, Bansal, Fisac, Tomlin. "FaSTrack: a Modular Framework for Fast and Guaranteed Safe Motion Planning." CDC, 2017.]

Robust Robot Planning with Human Predictions



Hamilton-Jacobi Reachability Analysis

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[Fisac, 2018]

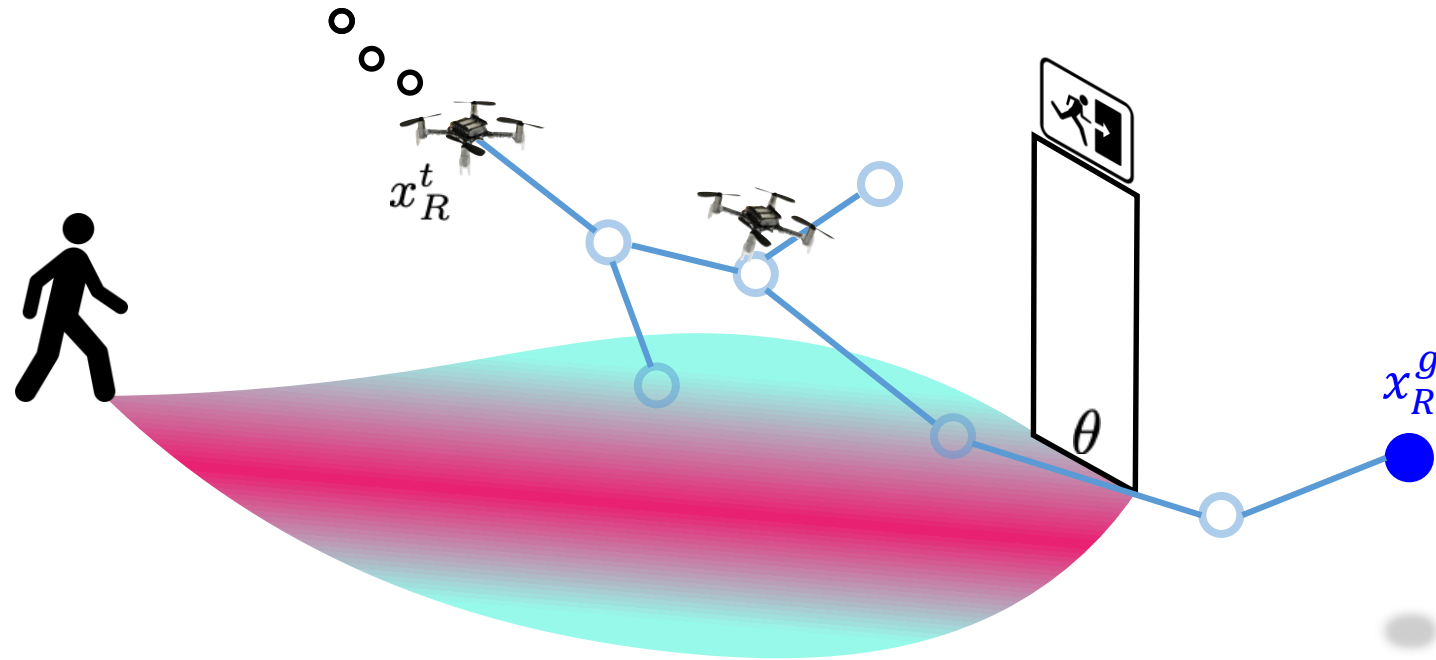
[Lygeros, 2005]

[Mitchell, 2005]

[Herbert, 2017]

Robust Robot Planning with Human Predictions

$$P(\text{Crash}(\text{drone})) > \textit{collision}_{\textit{thresh}}$$



[Fisac, 2018]

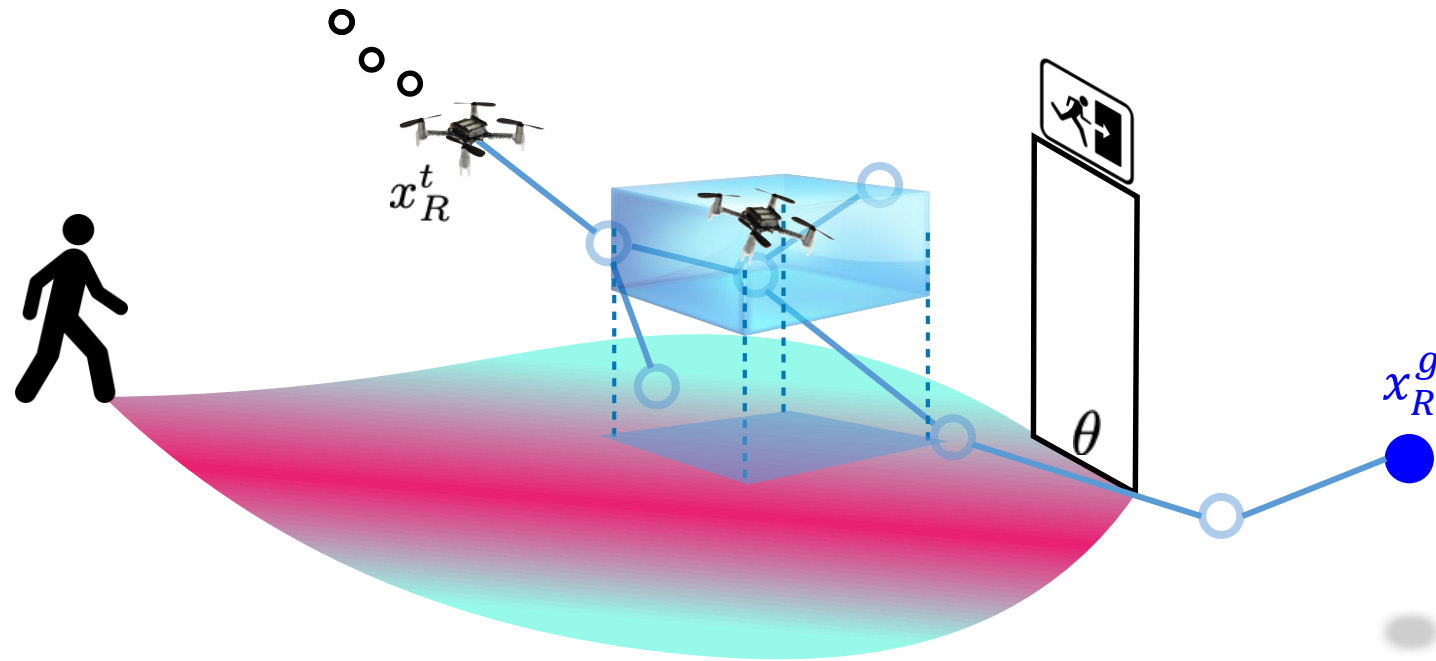
[Lygeros, 2005]

[Mitchell, 2005]

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Robust Robot Planning with Human Predictions

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[Fisac, 2018]

[Lygeros, 2005]

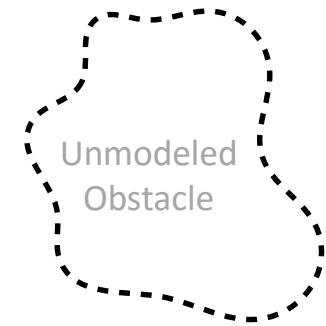
[Mitchell, 2008]

[Herbert, 2017]

What if the predictive model is *wrong*?

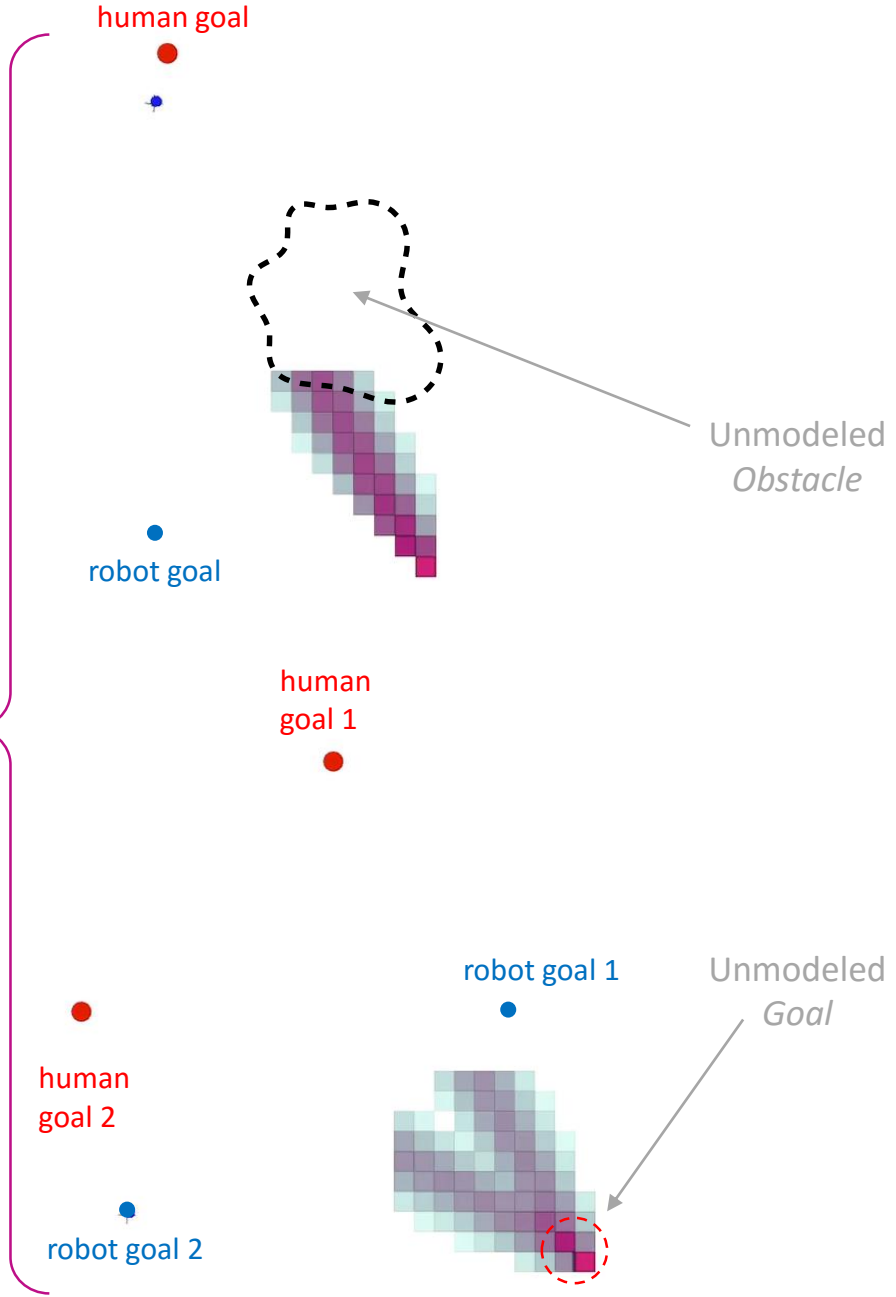


Modeled
human goal

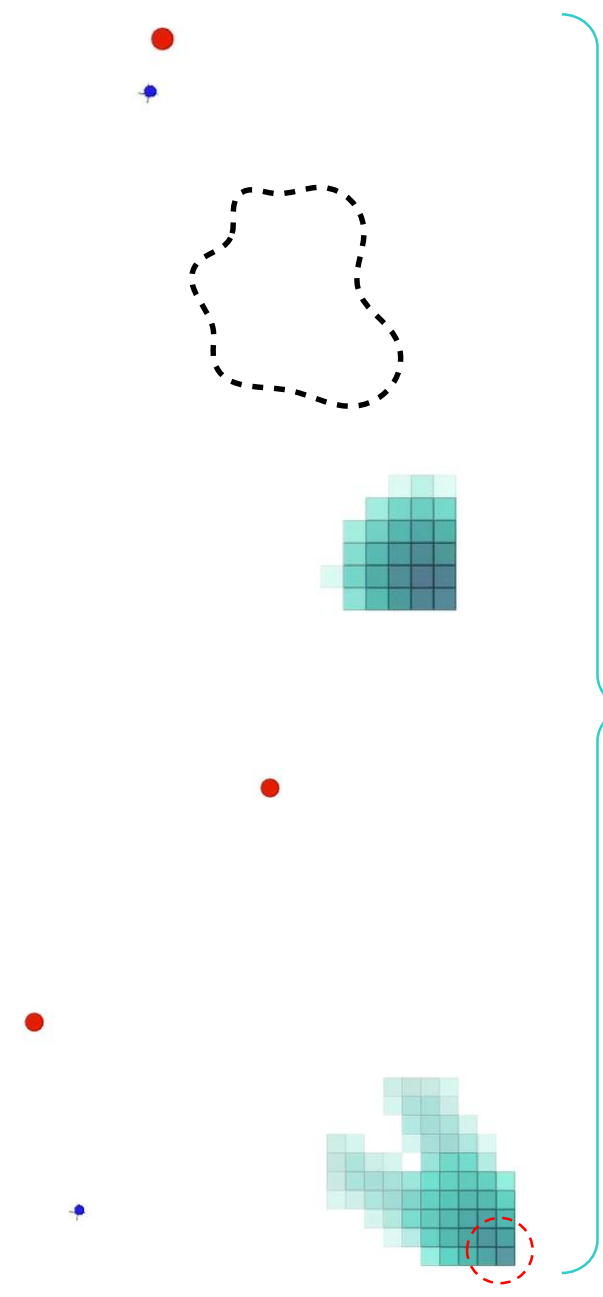


Robot goal

High Confidence



Low Confidence



Bayesian Model Confidence

$$P(u_H | x_H; \theta, \beta) \propto e^{\beta Q(x_H, u_H; \theta)}$$

$$\dot{x}_H = f_H(x_H, u_H)$$



Bayesian Model Confidence

$$P(u_H | x_H; \theta, \beta) \propto e^{\beta Q(x_H, u_H; \theta)}$$

$$\dot{x}_H = f_H(x_H, u_H)$$



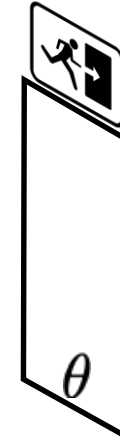
β

θ

Bayesian Model Confidence

$$P(\underline{u}_H \mid x_H; \theta, \underline{\beta}) \propto e^{\underline{\beta} Q(x_H, \underline{u}_H; \theta)}$$

$$\dot{x}_H = f_H(x_H, u_H)$$



Bayesian Model Confidence

$$P(u_H | x_H; \theta, \bar{\beta}) \propto e^{\bar{\beta} Q(x_H, u_H; \theta)}$$

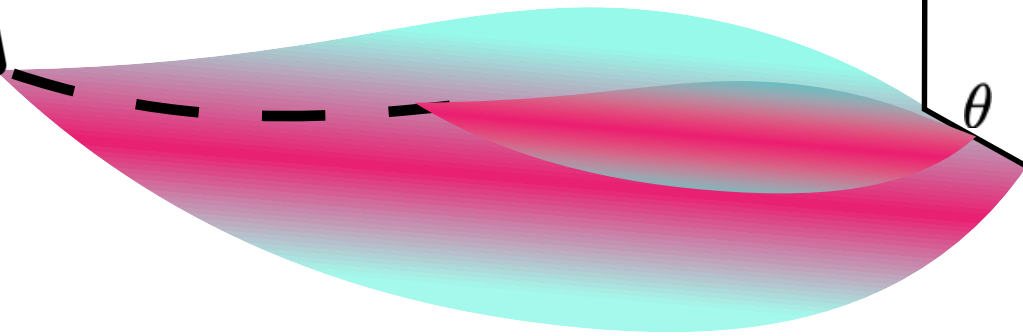
$$\dot{x}_H = f_H(x_H, u_H)$$



Bayesian Model Confidence

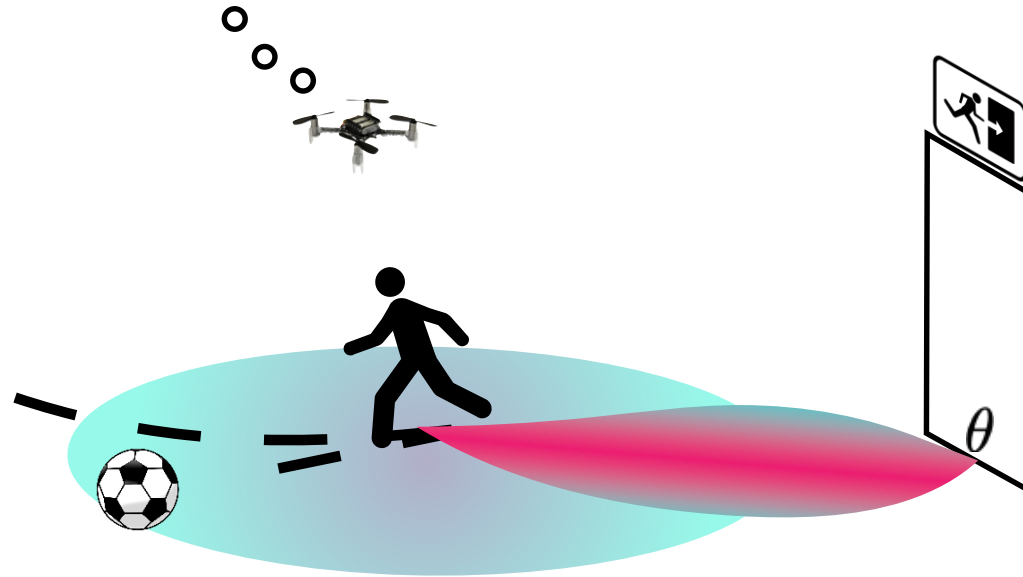
$$b^t(\beta) \propto P(u_H^t | x_H^t; \theta, \beta) b^{t-1}(\beta)$$

$$\dot{x}_H = f_H(x_H, u_H)$$

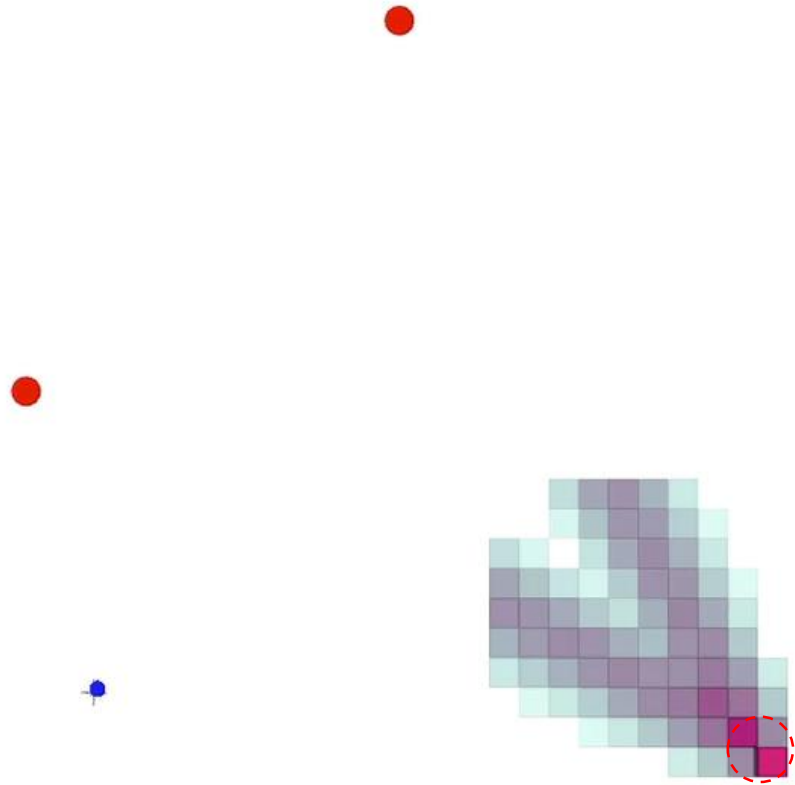


Bayesian Model Confidence

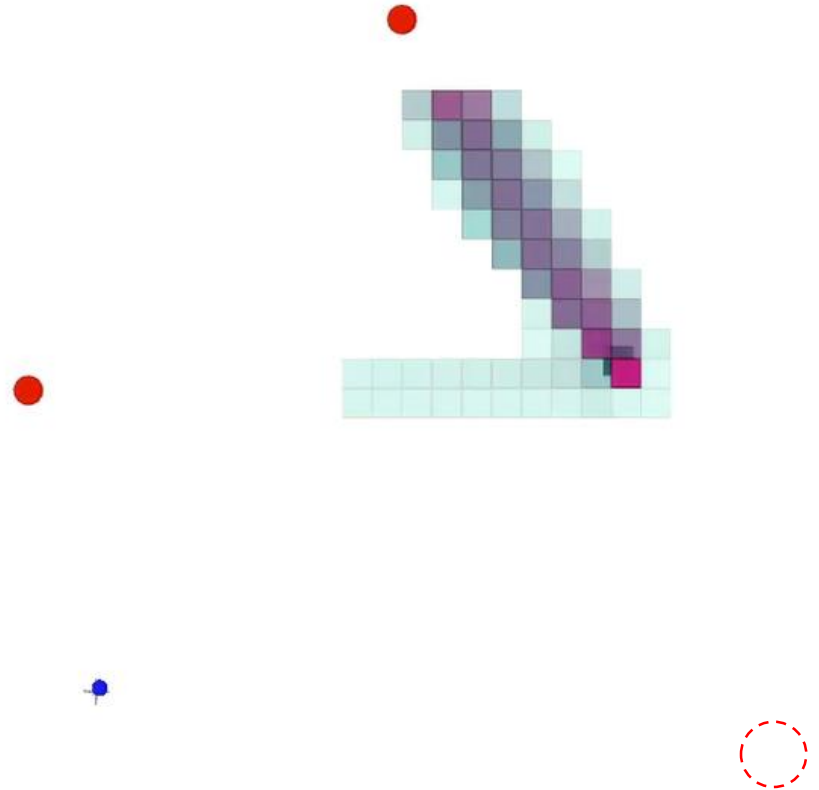
$$b^t(\beta) \propto P(u_H^t | x_H^t; \theta, \beta) b^{t-1}(\beta)$$



Fixed confidence $\bar{\beta}$



Bayesian confidence $b^t(\beta)$

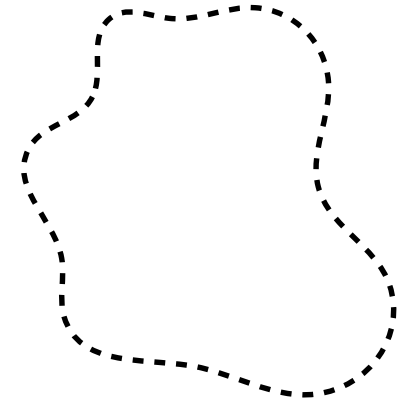




More confident!

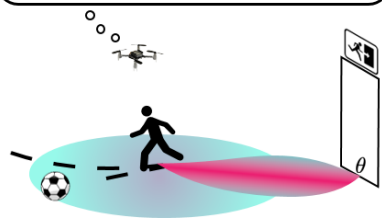


Less confident!



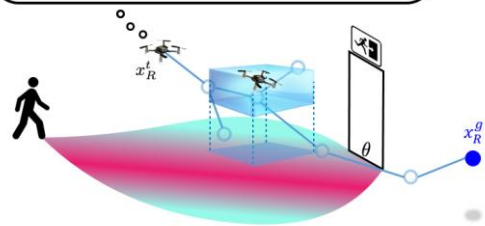
Confidence-aware prediction

$$b^t(\beta) \propto P(u_H^t | x_H^t; \theta, \beta) b^{t-1}(\beta)$$

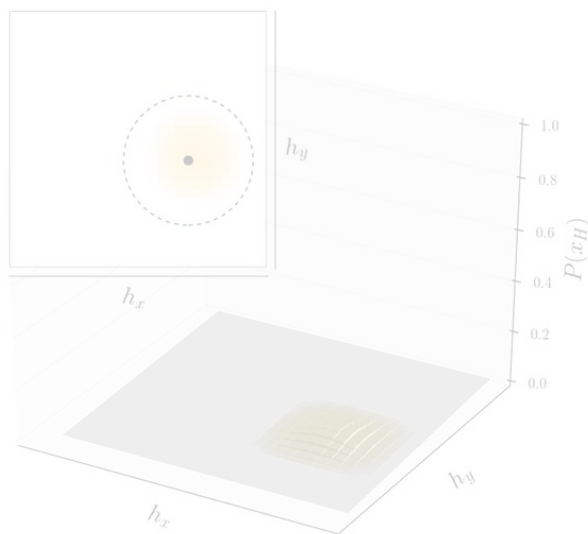


Robust motion planning

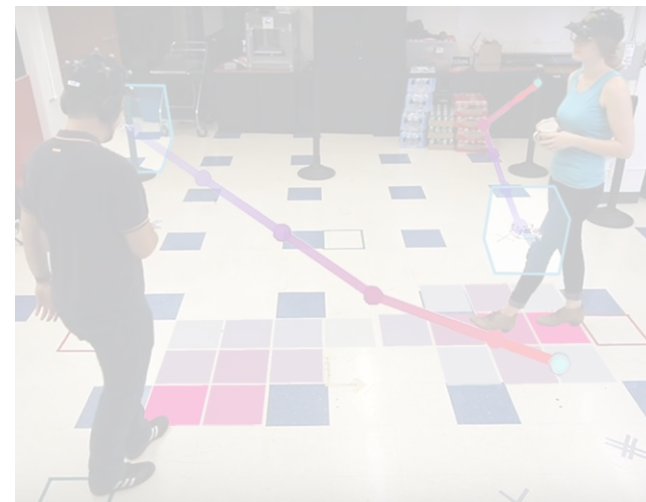
$$P(\text{Crash}(\text{robot})) > \text{collision}_{\text{thresh}}$$



Connections to reachability analysis

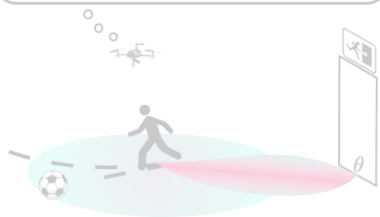


Scaling up to multi-robot, multi-human scenarios



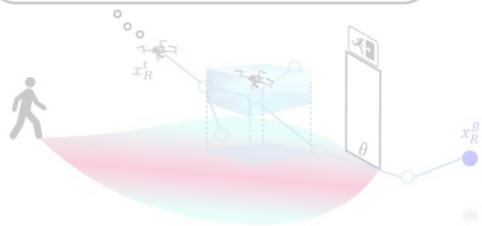
Confidence-aware prediction

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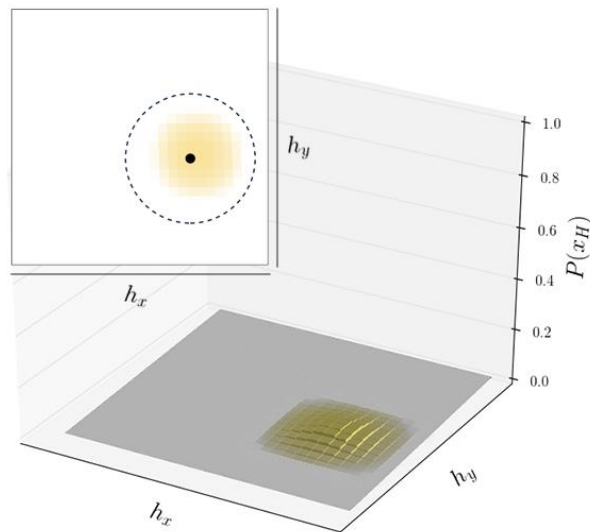


Robust motion planning

$$P(\text{Crash}(\text{drone})) > \text{collision}_{\text{thresh}}$$



Connections to reachability analysis

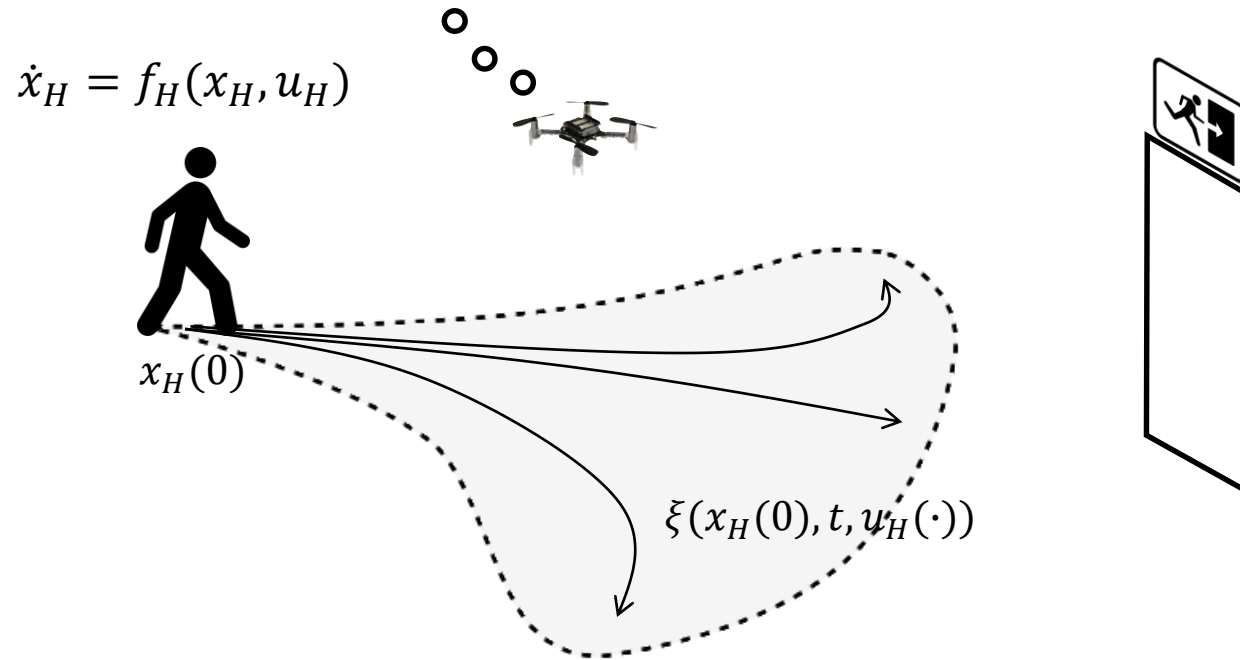


Scaling up to multi-robot, multi-human scenarios



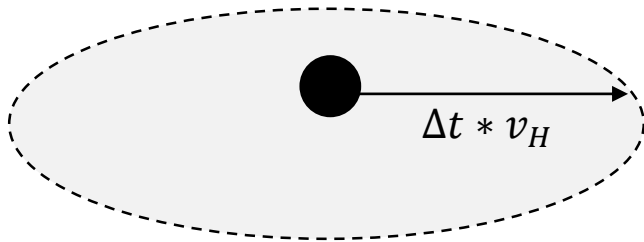
Forward Reachable Set

$$FRS(x_H, t) := \{x' : \exists u_H(\cdot), x' = \xi(x_H, t, u_H(\cdot))\}$$



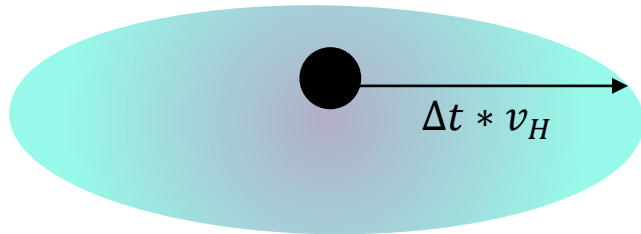
Forward Reachable Set

$$\dot{h}_x = v_H \cos(u_H)$$
$$\dot{h}_y = v_H \sin(u_H)$$



Forward Reachable Set

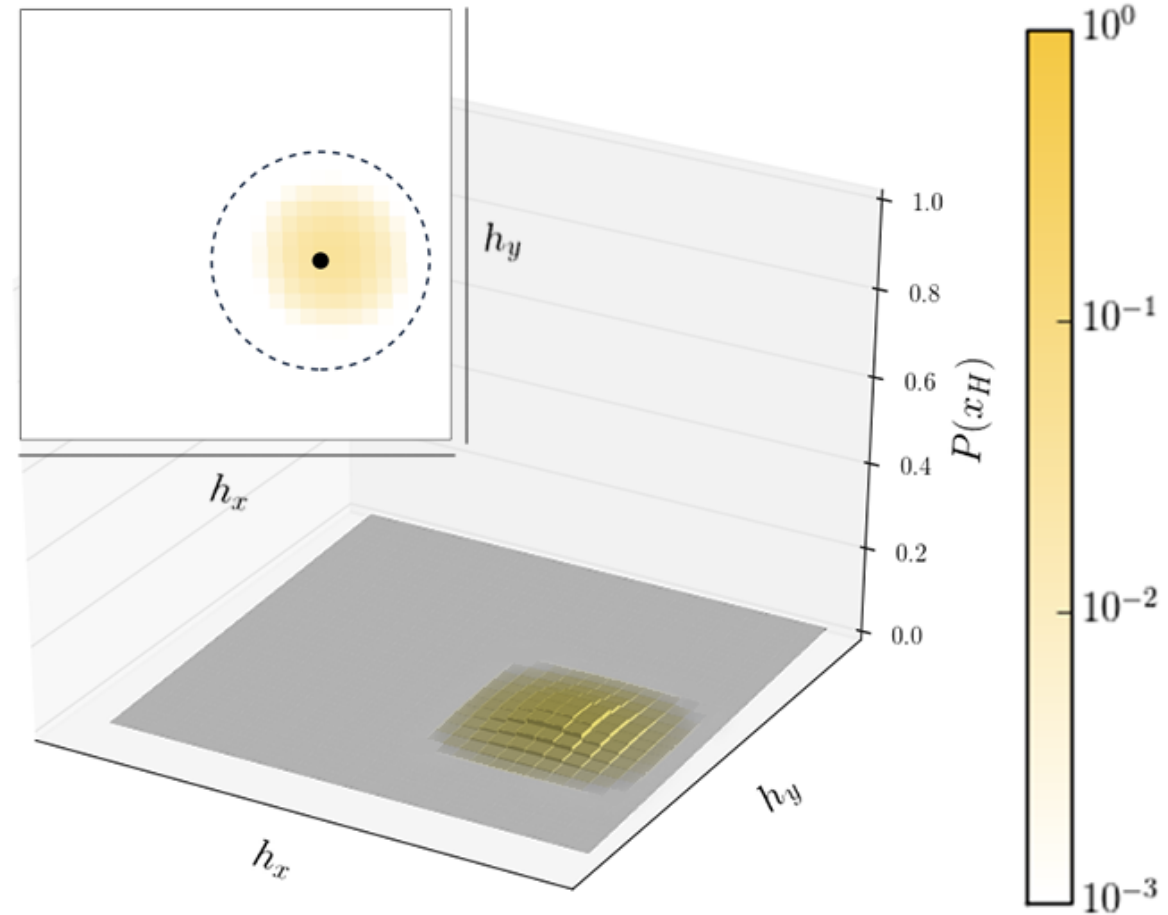
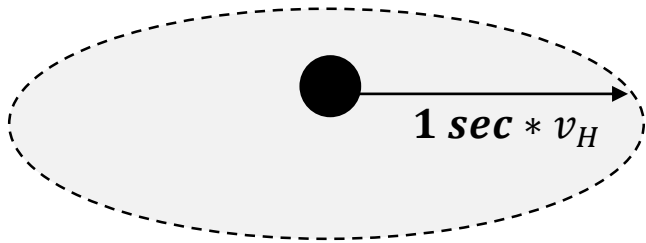
$$\dot{h}_x = v_H \cos(u_H)$$
$$\dot{h}_y = v_H \sin(u_H)$$



Forward Reachable Set

β -low State Distribution

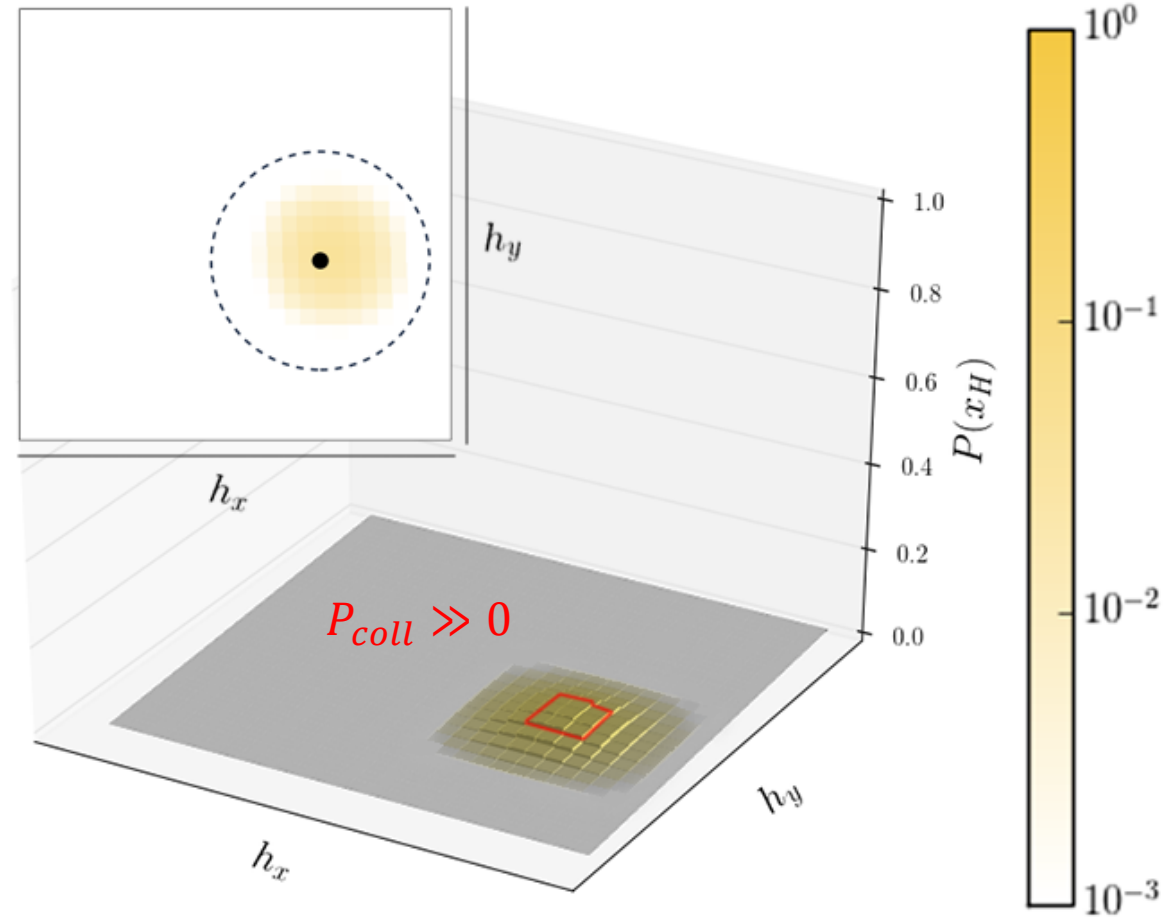
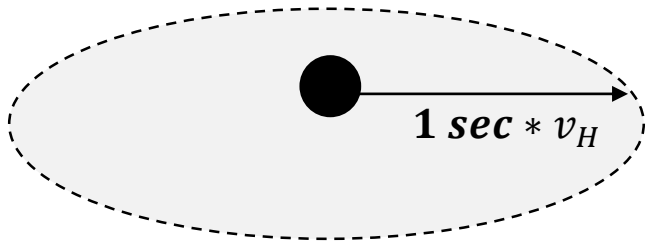
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Forward Reachable Set

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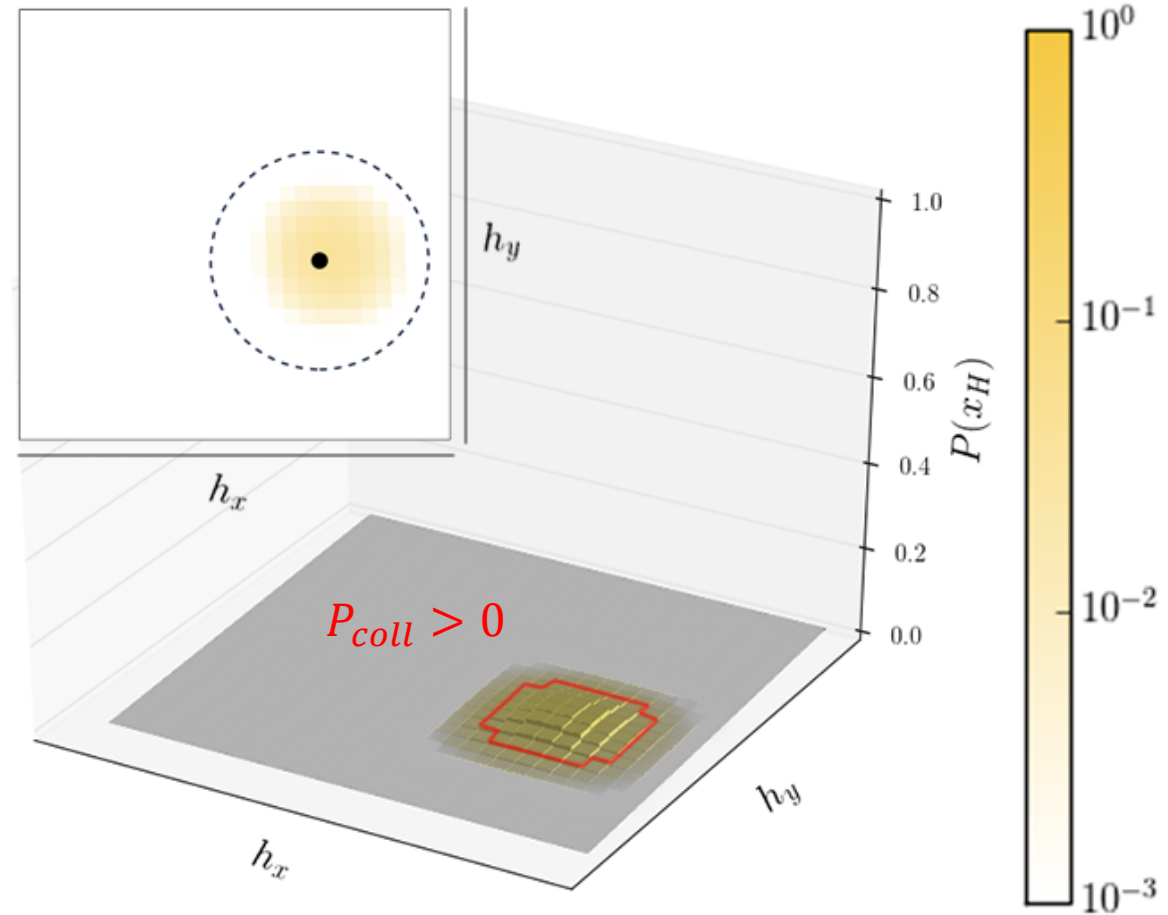
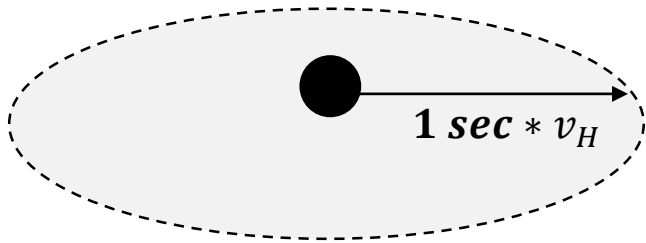
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Forward Reachable Set

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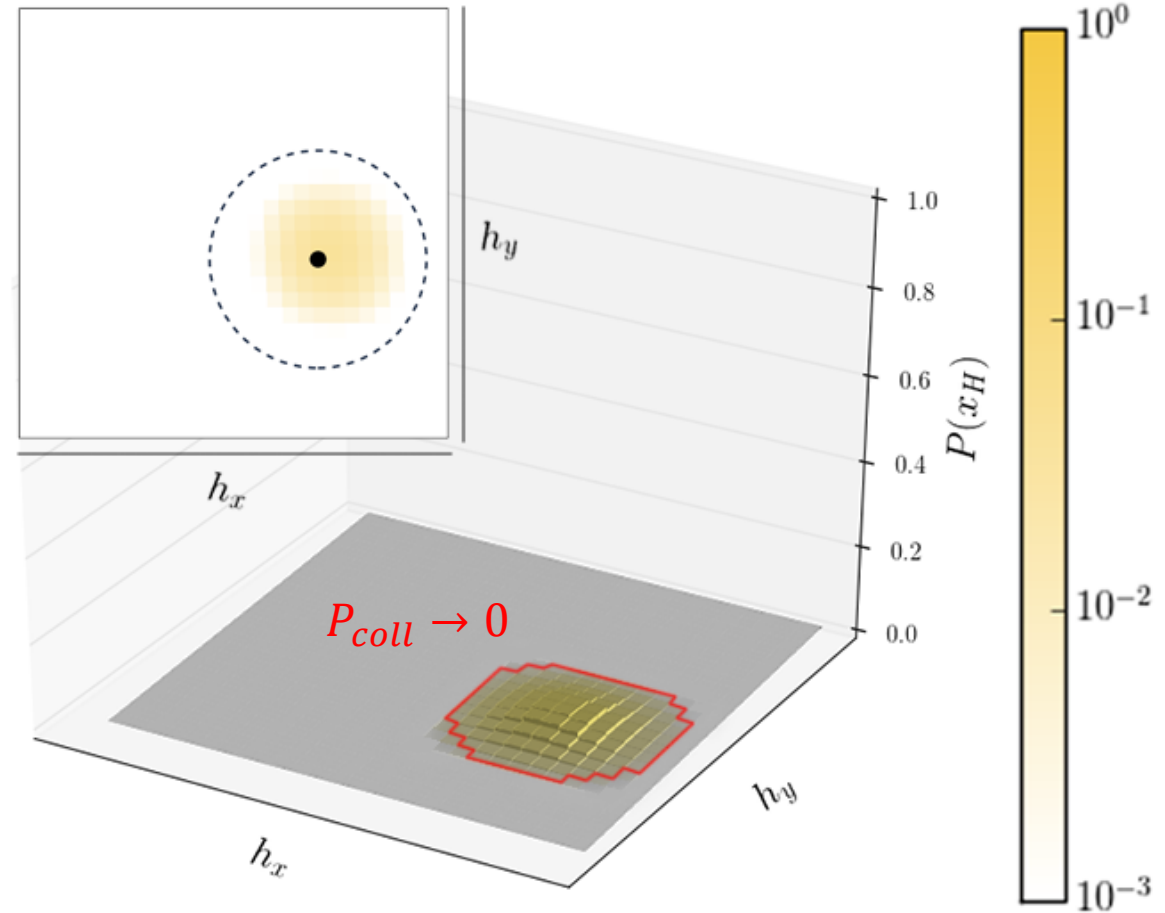
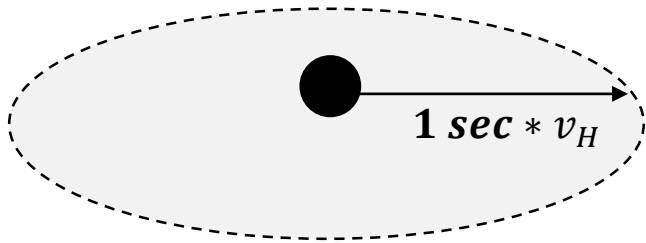
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Forward Reachable Set

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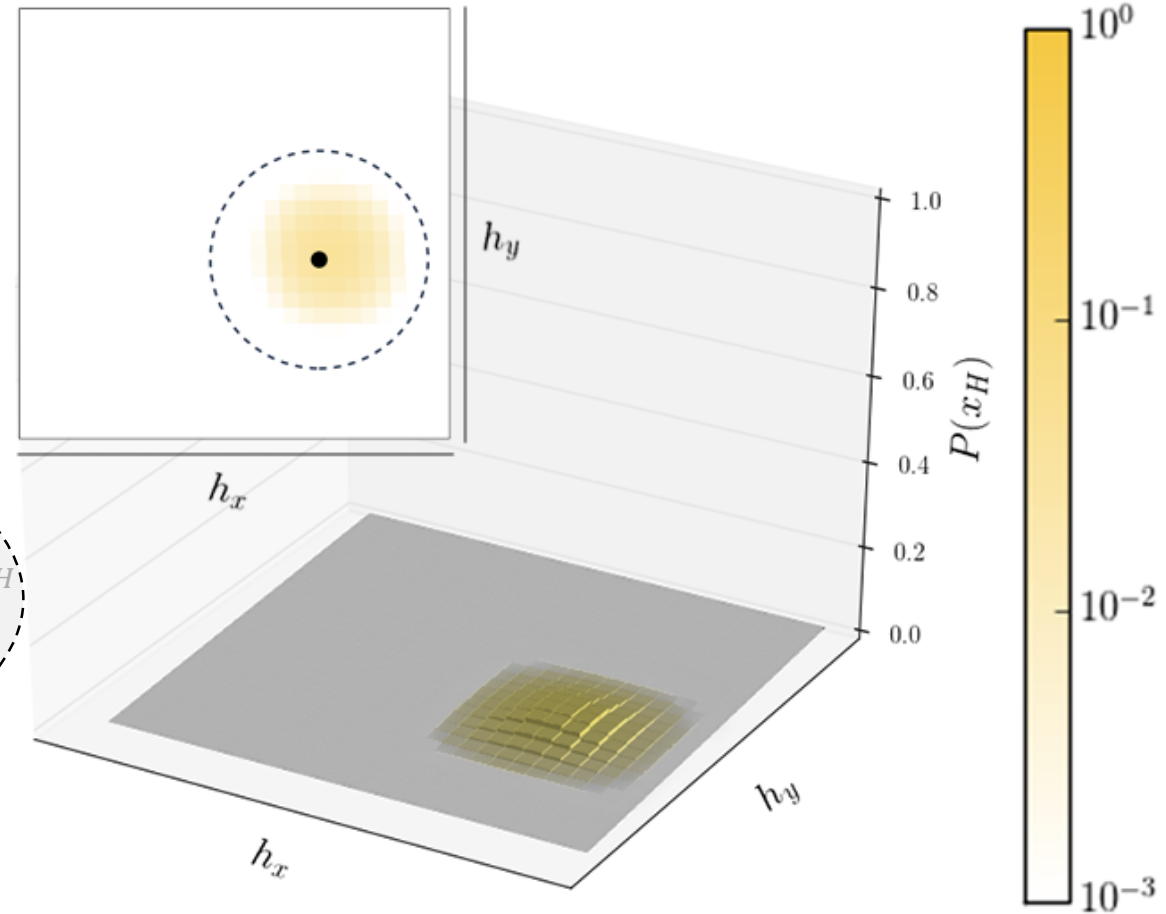
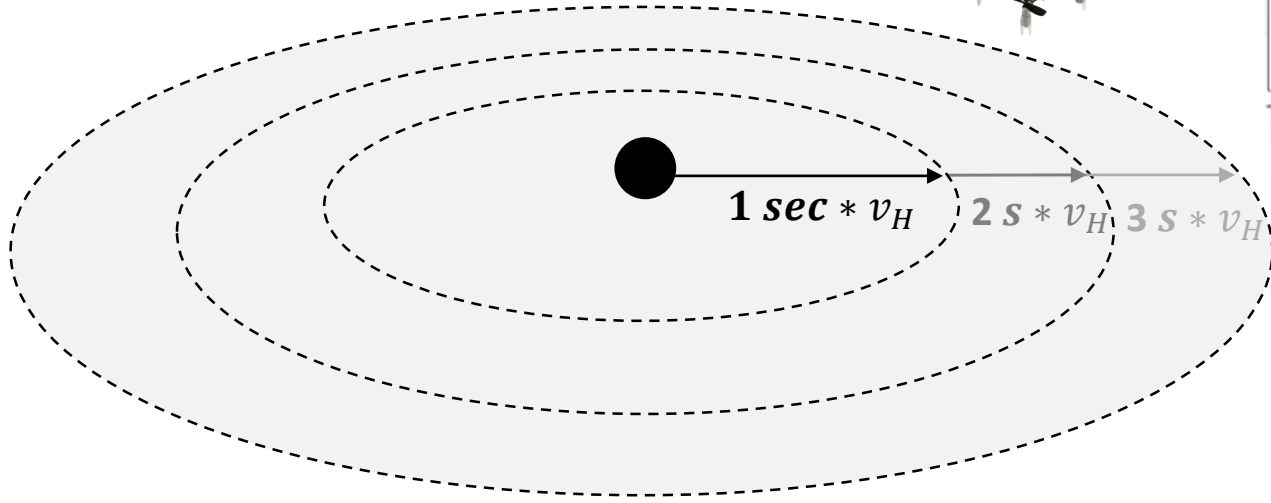
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Forward Reachable Set

β -low State Distribution

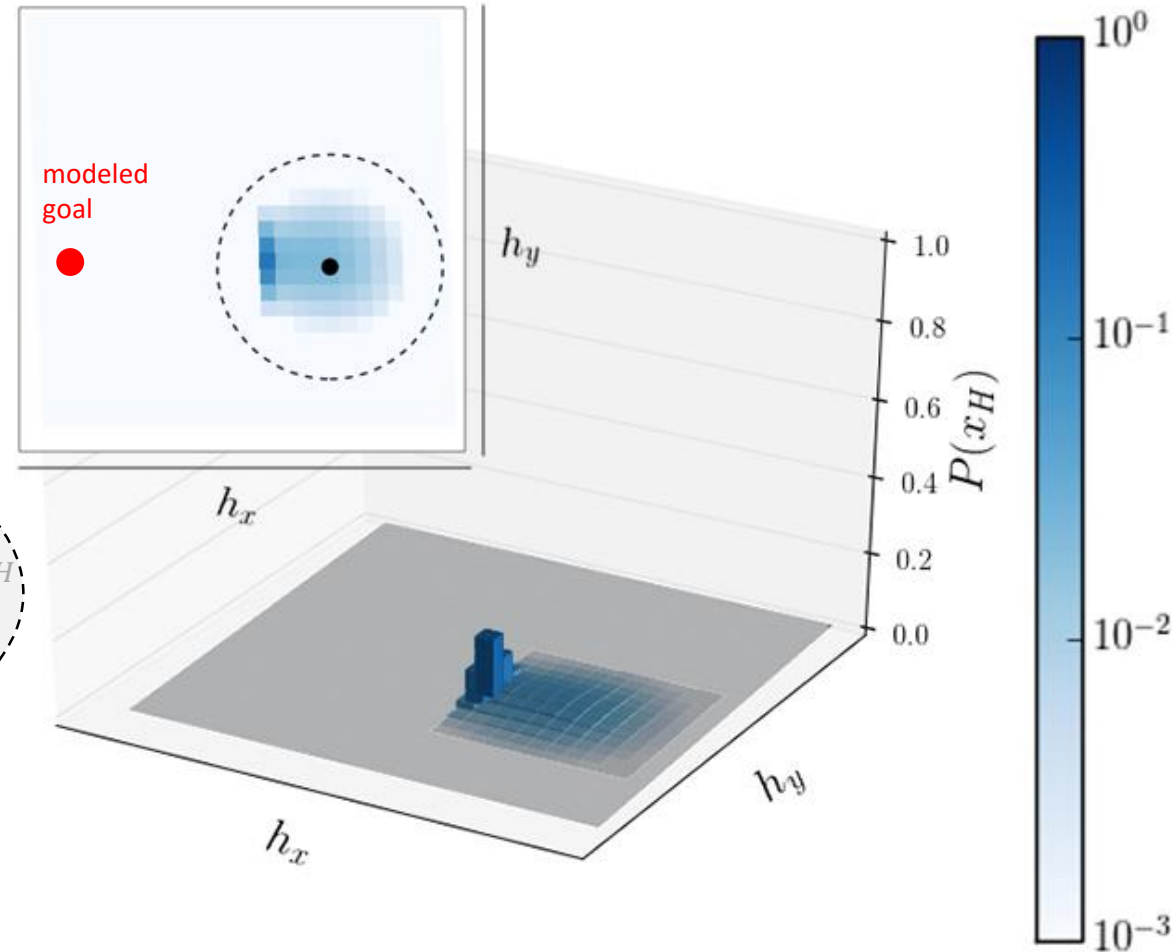
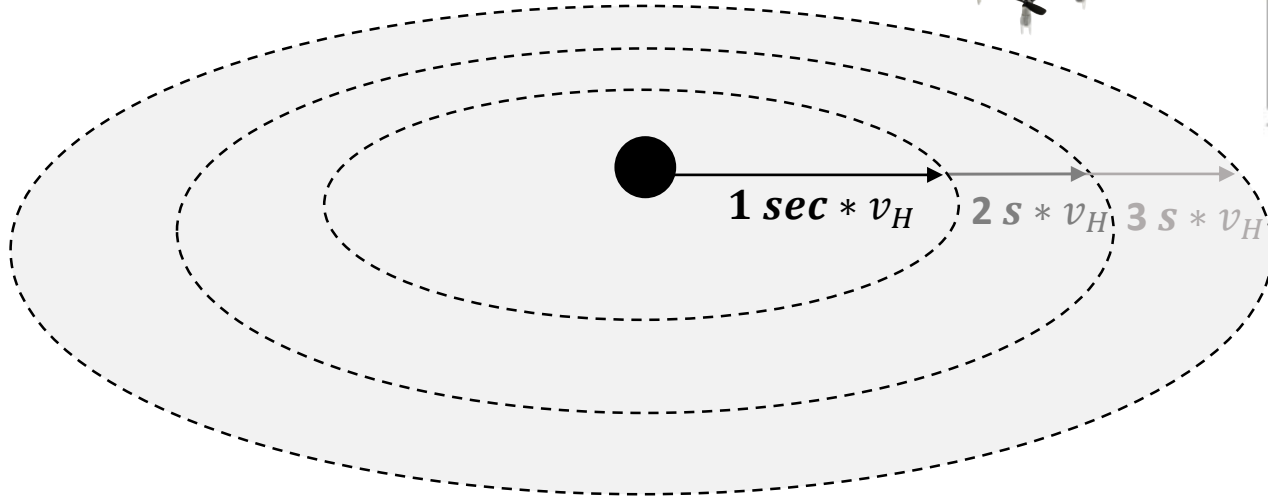
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Forward Reachable Set

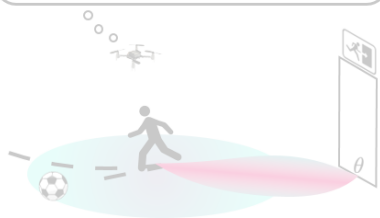
β -Bayes State Distribution

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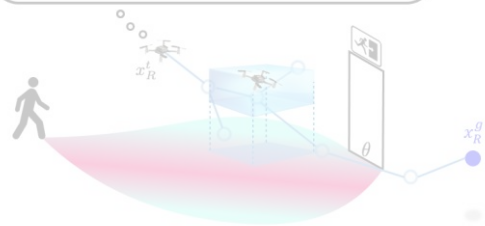
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$$b^t(\beta) \propto P(u_H^t | x_H^t; \theta, \beta) b^{t-1}(\beta)$$

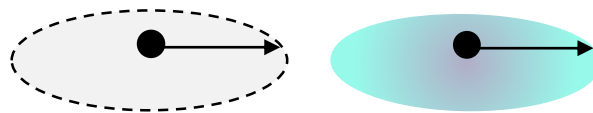


Robust motion planning

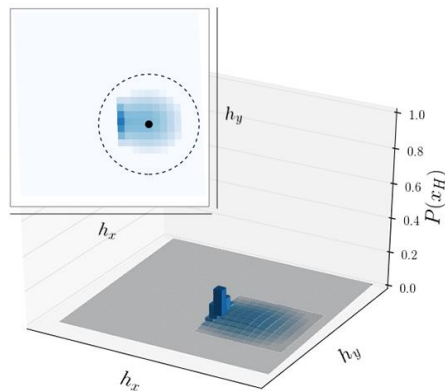
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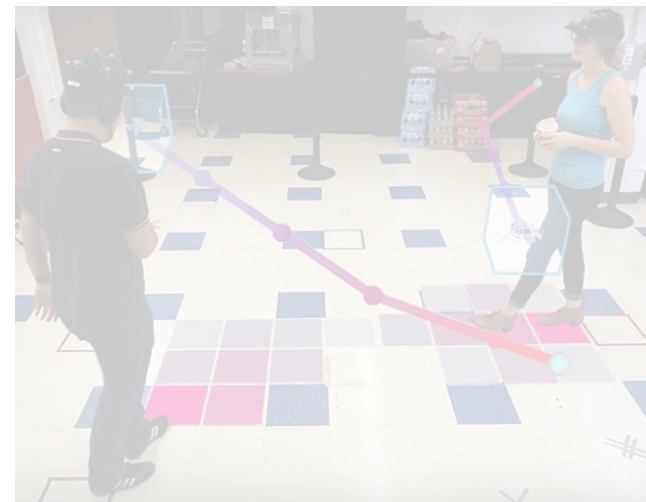
Connections between predictions and FRS



Confidently determining subsets of the FRS to avoid

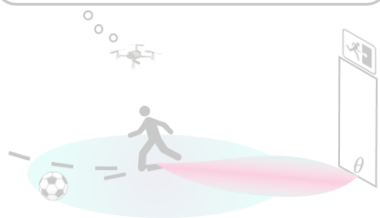


Scaling up to multi-robot, multi-human scenarios



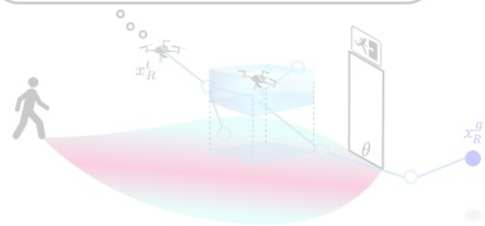
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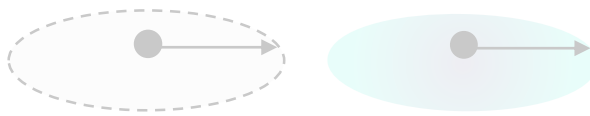


Robust motion planning

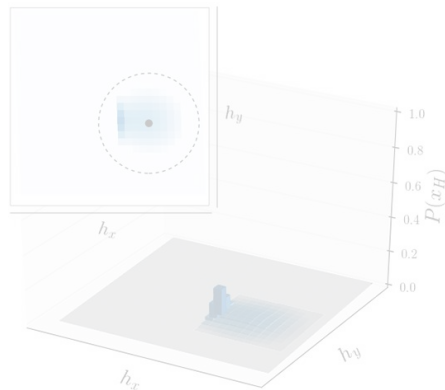
$$P(\text{Crash}(\text{robot})) > \text{collision}_{\text{thresh}}$$



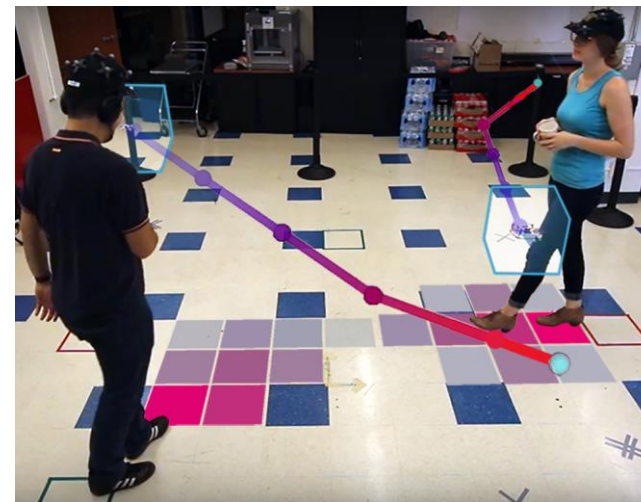
Connections between predictions and FRS

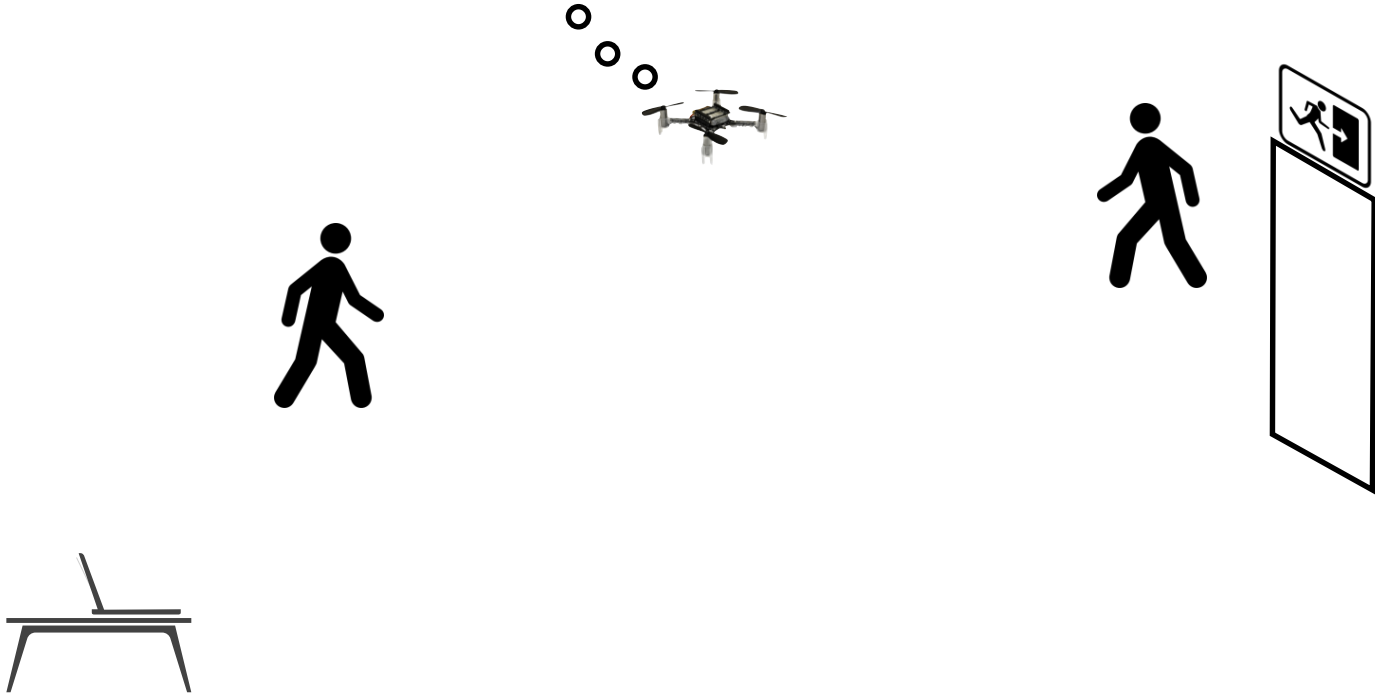
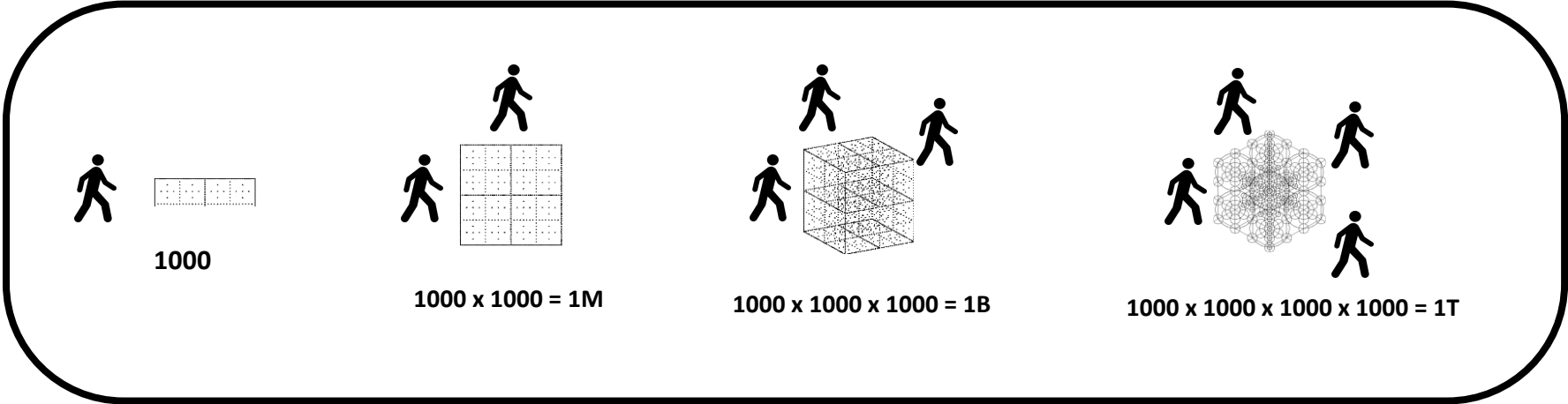


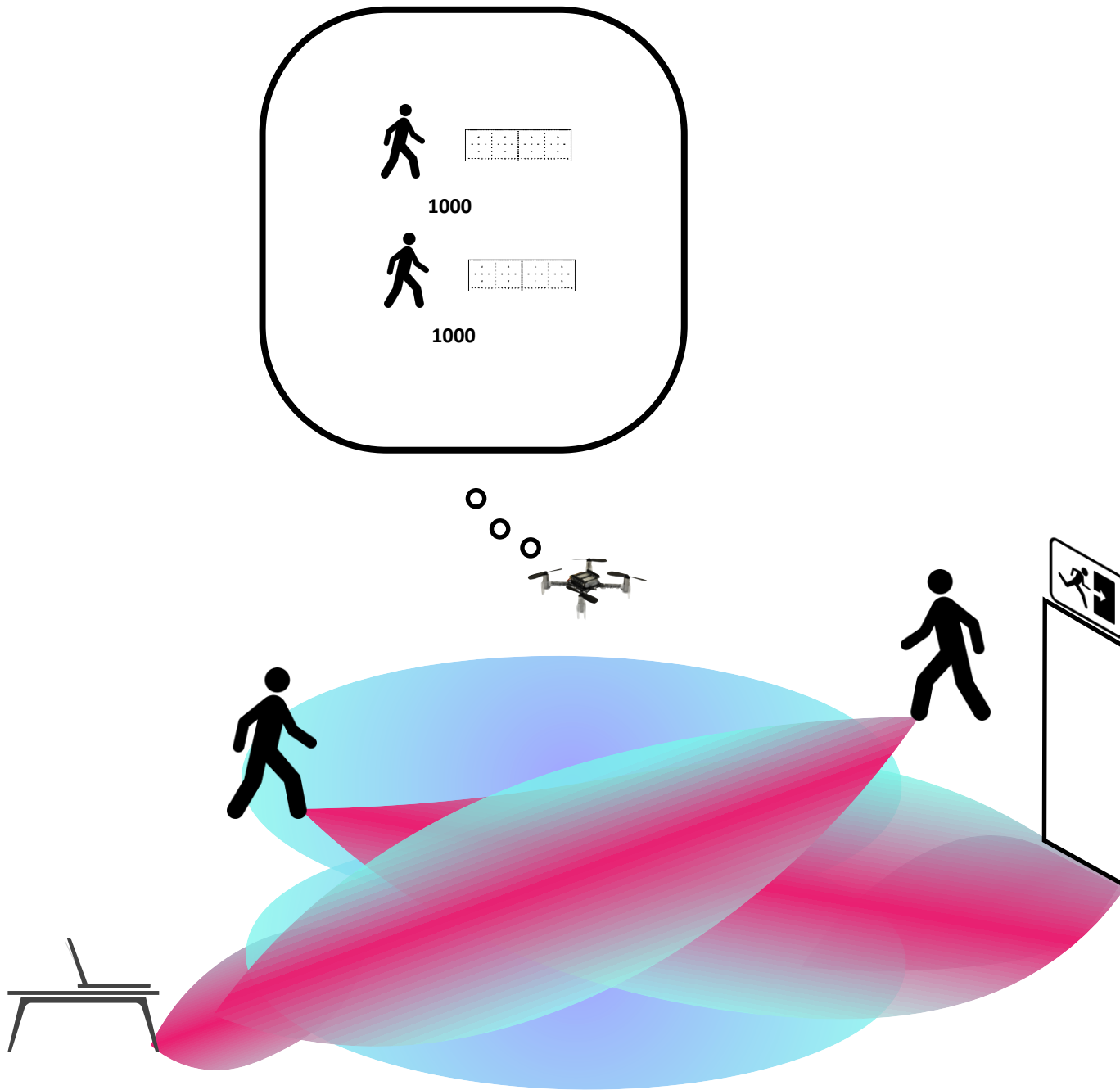
Determining subsets of the FRS to avoid

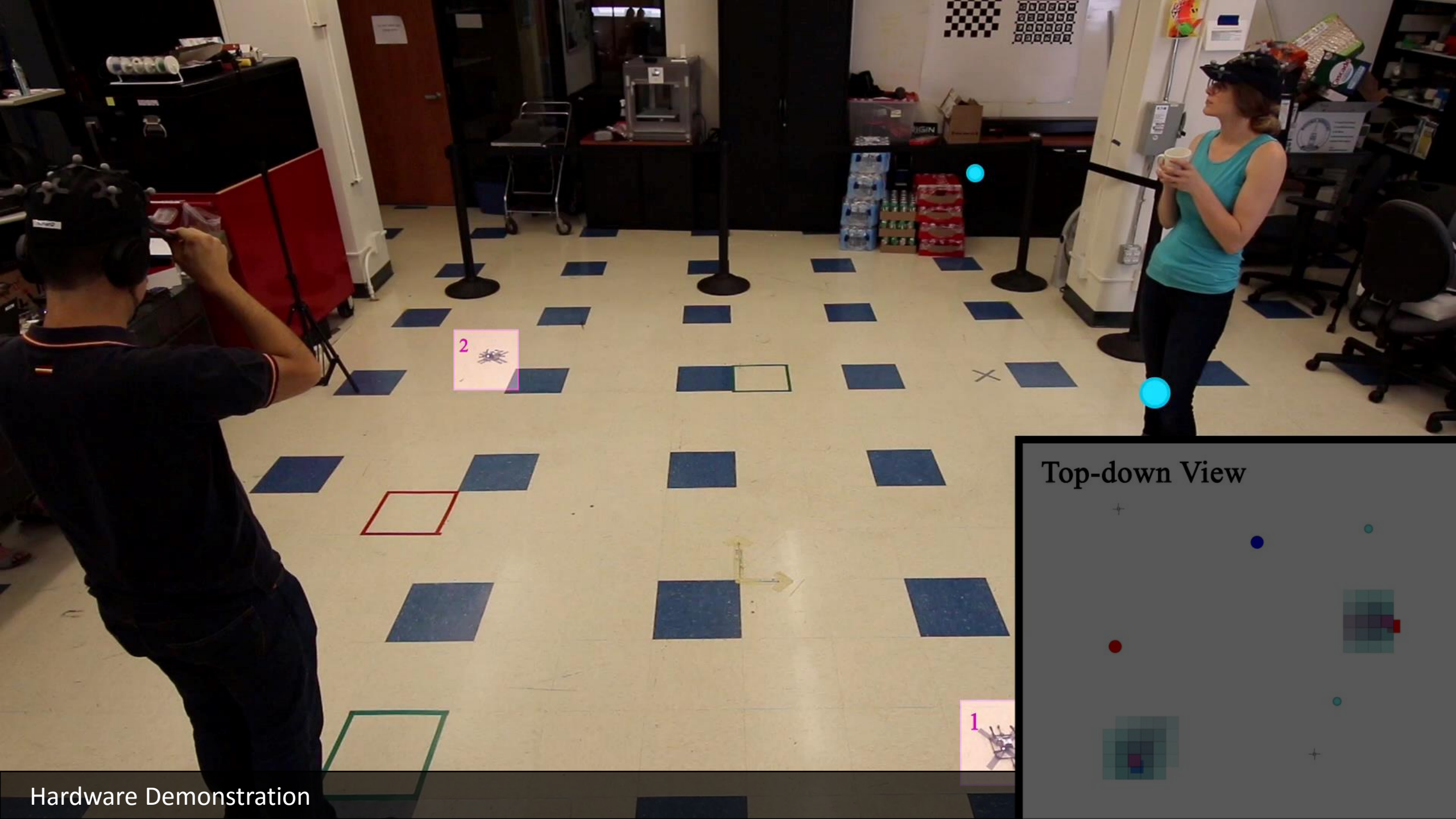


Scaling up to multi-robot, multi-human scenarios









2

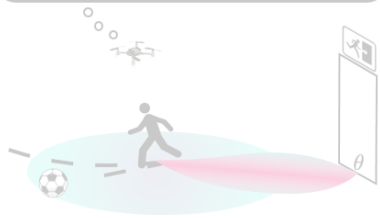
1

Top-down View

Hardware Demonstration

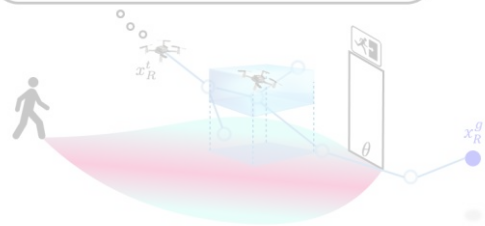
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Robust motion planning

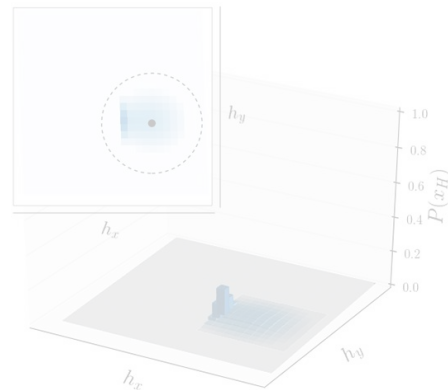
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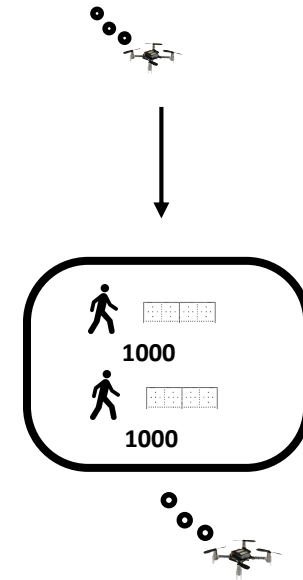
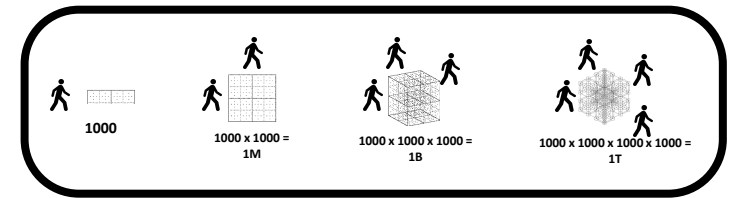
Connections between predictions and FRS



Determining subsets of the FRS to avoid

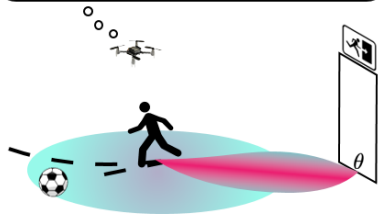


Confidence-aware predictions offer promising directions for scaling



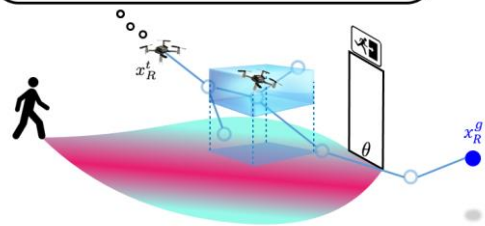
Confidence-aware prediction

$$b^t(\beta) \propto P(u_H^t | x_H^t; \theta, \beta) b^{t-1}(\beta)$$

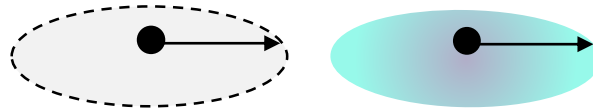


Robust motion planning

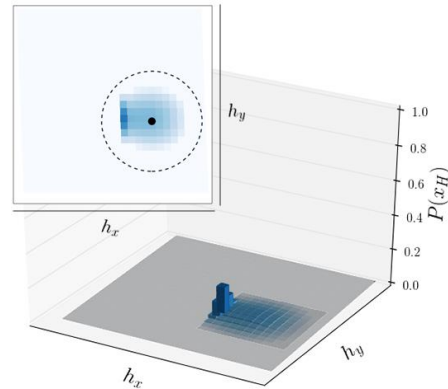
$$P(\text{Crash}(\text{drone})) > \text{collision}_{\text{thresh}}$$



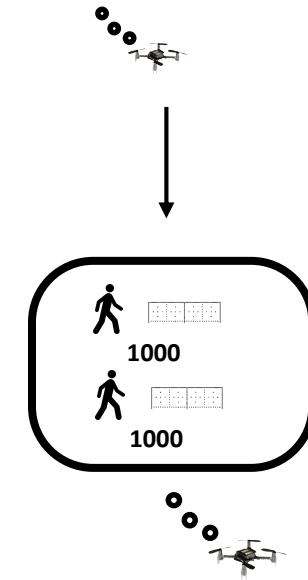
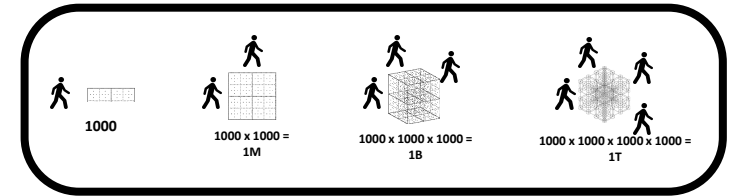
Connections between predictions and FRS

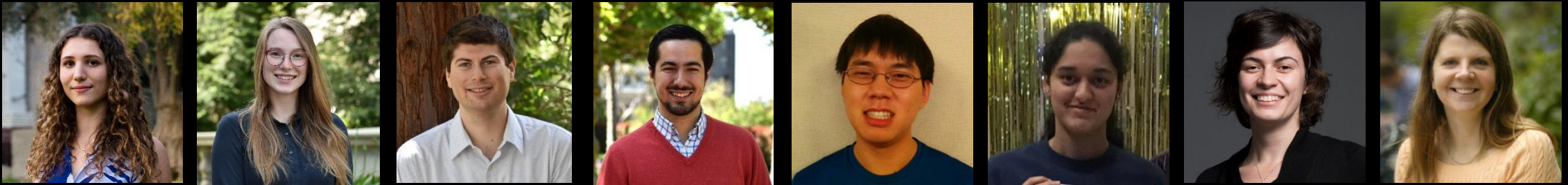


Determining subsets of the FRS to avoid



Confidence-aware predictions offer promising directions for scaling





Papers

Fisac*, Bajcsy*, Herbert, Fridovich-Keil, Wang, Tomlin, and Dragan. "Probabilistically Safe Robot Planning with Confidence-Based Human Predictions." RSS, 2018.

Fridovich-Keil*, Bajcsy*, Fisac, Herbert, Wang, Dragan, and Tomlin. "Confidence-Aware Motion Prediction for Real-Time Collision Avoidance." IJRR, 2019

Bajcsy*, Herbert*, Fridovich-Keil, Fisac, Deglurkar, Dragan, and Tomlin, "A Scalable Framework for Real-Time Multi-Robot, Multi-Human Collision Avoidance." ICRA, 2019.

Herbert*, Chen*, Han, Bansal, Fisac, Tomlin. "FaSTrack: a Modular Framework for Fast and Guaranteed Safe Motion Planning." CDC, 2017.

Code

Multi-robot, multi-human planning: <https://github.com/HJReachability/faSTPeople>

Fast and safe robot tracking: <https://github.com/HJReachability/fastrack>

Pedestrian prediction: https://github.com/shwang/pedestrian_prediction

ROS wrapper for pedestrian prediction: https://github.com/abajcsy/crazyflie_human